

1147-13-801

**Paul Baginski\*** ([pbaginski@fairfield.edu](mailto:pbaginski@fairfield.edu)), Dept. of Mathematics, Fairfield University, 1073 North Benson Rd., Fairfield, CT 06824. *Nonunique factorization in the ring of integer-valued polynomials.*

The ring of integer-valued polynomials  $\text{Int}(\mathbb{Z})$  is the set of polynomials with rational coefficients which produce integer values for integer inputs. Specifically,

$$\text{Int}(\mathbb{Z}) = \{f(x) \in \mathbb{Q}[x] \mid \forall n \in \mathbb{Z} \ f(n) \in \mathbb{Z}\}.$$

$\text{Int}(\mathbb{Z})$  constitutes an interesting example in algebra from many perspectives; for example, it is a natural example of a non-Noetherian ring. It is also a ring with nonunique factorization. It is a finite factorization domain with infinite elasticity. Frisch recently demonstrated that in  $\text{Int}(\mathbb{Z})$ , you can find an element  $f(x)$  that has any factorization lengths you desire and you can even prescribe the number of factorizations of each length. The polynomials constructed in this way have high degree. We give a graded analysis, determining all the possible elasticities and catenary degrees for a polynomial as a function of the degree of the polynomial.

Joint work with: Greg Knapp, Jad Salem, and Gabrielle Scullard. (Received January 28, 2019)