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**Samantha N Petti\*** (spetti@gatech.edu) and **Santosh S Vempala**. *Approximating Sparse Graphs: The Random Overlapping Communities Model*.

How can we approximate sparse graphs and sequences of sparse graphs (with average degree unbounded and  $o(n)$ )? We consider convergence in the first  $k$  moments of the graph spectrum (equivalent to the numbers of closed  $k$ -walks) appropriately normalized. We introduce a simple random graph model that captures the limiting spectra of many sequences of interest, including the sequence of hypercube graphs. The Random Overlapping Communities (ROC) model is specified by a distribution on pairs  $(s, q)$ ,  $s \in \mathbb{Z}_+$ ,  $q \in (0, 1]$ . A graph on  $n$  vertices with average degree  $d$  is generated by repeatedly picking pairs  $(s, q)$  from the distribution, adding an Erdős-Rényi random graph of edge density  $q$  on a subset of vertices chosen by including each vertex with probability  $s/n$ , and repeating this process so that the expected degree is  $d$ . Our proof of convergence to a ROC random graph is based on the Stieltjes moment condition. The model is an effective approximation for individual graphs. For almost all possible triangle-to-edge and four-cycle-to-edge ratios, there exists a pair  $(s, q)$  such that the ROC model with this single community type produces graphs with both desired ratios, a property that cannot be achieved by block models of bounded size. (Received February 10, 2018)