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**Norisuke Ioku\*** (ioku@ehime-u.ac.jp). *Canceling effects in higher-order Hardy-Sobolev inequalities.*

A classical Hardy-Sobolev type inequality involving weighted norms depending on powers of the distance function from the boundary  $d(x)$  asserts that if  $\Omega$  is a bounded Lipschitz domain, and  $\alpha \neq p - 1$ , then there exists a constant  $C$  such that

$$\left\| \frac{u}{d} \right\|_{L^p(\Omega, d^\alpha)} \leq C (\|u\|_{L^p(\Omega, d^\alpha)} + \|\nabla u\|_{L^p(\Omega, d^\alpha)}) \quad (1)$$

for every  $u \in C_0^\infty(\Omega)$ , where  $\|u\|_{L^p(\Omega, d^\alpha)} := \left( \int_\Omega d(x)^\alpha |u(x)|^p dx \right)^{\frac{1}{p}}$ . On the other hand, inequality (1) fails for the critical value  $\alpha = p - 1$ . The main purpose of this talk is to show that, this notwithstanding, suitable higher-order versions of inequality (1), which cannot just be obtained from (1) via iteration, do hold even when  $\alpha = p - 1$ .

This is a joint work with Professor Andrea Cianchi (University of Florence). (Received February 08, 2018)