I will describe some invariants for braids, knots, and links arising from ideas in quantum topology, and connect their study to classical questions about complexity of smoothly-imbedded surfaces in the 4-ball. Along the way, we will survey the ways in which key representation-theoretic features of the invariant track topological information. (Received July 31, 2018)