

1143-05-353

**Tao Jiang\*** ([jiangt@miamioh.edu](mailto:jiangt@miamioh.edu)), Department of Mathematics, Miami University, Oxford, OH 45056, and **Jie Ma** ([jiema@ustc.edu.cn](mailto:jiema@ustc.edu.cn)) and **Liana Yepremyan** ([liana.yepremyan@maths.ox.ac.uk](mailto:liana.yepremyan@maths.ox.ac.uk)). *On Turán exponents of bipartite graphs.*

Given a family  $\mathcal{F}$  of graphs, the Turán number  $ex(n, \mathcal{F})$  is the maximum number of edges in an  $n$ -vertex graph that does not contain any member of  $\mathcal{F}$  as a subgraph. Verifying an old conjecture of Erdős and Simonovits (and reiterated by Frankl and Füredi and Simonovits), Bukh and Conlon showed that for each rational number  $r$  with  $1 < r < 2$  there exists a family  $\mathcal{F}$  of bipartite graphs such that  $ex(n, \mathcal{F}) = \Theta(n^r)$ .

A related conjecture of Erdős and Simonovits asks if for each rational number  $r$  with  $1 < r < 2$  there exists a single bipartite graph  $H$  such that  $ex(n, H) = \Theta(n^r)$ . This conjecture is still wide open. Until recently the conjecture was only verified for  $r = 1 + 1/k$  and  $r = 2 - 1/k$  where  $k$  is an integer at least 2, achieved by so-called theta graphs and complete bipartite graphs, respectively. In this talk, we show that the answer to the Erdős-Simonovits question is affirmative for all rational numbers  $r$  of the form  $4k/(2k + 1)$ , where  $k$  is a positive integer, and for  $r = 7/5$ . Our first theorem also answers a question of Pinchasi and Sharir on graphs related to the cubes. This provides infinitely many new bipartite graphs  $H$  for which the order of magnitude of  $ex(n, H)$  is determined. (Received August 18, 2018)