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Mark Ellingham* (mark.ellingham@vanderbilt.edu), **Pouria Salehi Nowbandegani** and **Songling Shan**. *Toughness and prism-hamiltonicity of P_4 -free graphs.*

The *prism* over a graph G is the product $G \square K_2$, i.e., the graph obtained by taking two copies of G and adding a perfect matching joining the two copies of each vertex by an edge. The graph G is called *prism-hamiltonian* if it has a hamiltonian prism. Jung showed that every 1-tough P_4 -free graph with at least three vertices is hamiltonian. We extend this to observe that for $k \geq 1$ a P_4 -free graph has a spanning k -walk (closed walk using each vertex at most k times) if and only if it is $(1/k)$ -tough. As our main result, we show that for the class of P_4 -free graphs, the three properties of being prism-hamiltonian, having a spanning 2-walk, and being $(1/2)$ -tough are all equivalent. (Received January 27, 2019)