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**Linda Eroh, Cong X. Kang and Eunjeong Yi\*** (yie@tamug.edu). *The connected metric dimension at a vertex of a graph.*

The metric dimension is a well-studied notion in graph theory. We begin a local analysis of this notion by introducing *the connected metric dimension of  $G$  at a vertex  $v$* : a set of vertices  $S$  of a graph  $G$  is a *resolving set* if, for any pair of distinct vertices  $x$  and  $y$  of  $G$ , there is a vertex  $z \in S$  such that the distance between  $z$  and  $x$  is distinct from the distance between  $z$  and  $y$  in  $G$ . We say that a resolving set  $S$  is *connected* if  $S$  induces a connected subgraph of  $G$ . The *connected metric dimension of  $G$  at a vertex  $v$* , denoted by  $\text{cdim}_G(v)$ , is the minimum of the cardinalities of all connected resolving sets of  $G$  which contain the vertex  $v$ . The *connected metric dimension of  $G$* , denoted by  $\text{cdim}(G)$ , is  $\min\{\text{cdim}_G(v) : v \in V(G)\}$ . In this talk, we will consider, among others, the following aspects of the connected metric dimension: 1) the existence of a pair  $(G, v)$  such that  $\text{cdim}_G(v)$  takes all positive integer values from  $\text{dim}(G)$  to  $|V(G)| - 1$ , as  $v$  varies in a fixed graph  $G$ ; 2) the characterization of graphs  $G$  and their vertices  $v$  satisfying  $\text{cdim}_G(v) \in \{1, |V(G)| - 1\}$ ; 3) the planarity implication of the condition  $\text{cdim}(G) = 2$ . (Received January 06, 2019)