Given a hyperbolic 3- manifold which fibers over the circle with hyperbolic surface fiber, the inclusion map between the fiber and the manifold can be extended continuously to a map, resulting in a space-filling Peano curve. This type of continuous extension of a map to between corresponding boundaries is called a Cannon-Thurston map. Using Birman exact sequence for mapping class groups, we will explain how to construct a Cannon-Thurston map for the boundary of ‘surviving’ curve complex of a surface with punctures. This is a joint work with Christopher J. Leininger and Witsarut Pho-on. (Received August 13, 2019)