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**Joehyun Kim\*** (joehyunkim5@gmail.com), **Kelvin Kim** and **Jeewoo Lee**. *The Largest Angle Bisection Procedure*.

For a given triangle  $\Delta ABC$ , with  $\angle A \geq \angle B \geq \angle C$ , the largest angle bisection procedure consists in constructing  $AD$ , the angle bisector of angle  $\angle A$ , and replacing  $\Delta ABC$  by the two newly formed triangles,  $\Delta ABD$  and  $\Delta ACD$ . Let  $\Delta_{01}$  be a given triangle. Bisect  $\Delta_{01}$  into two triangles,  $\Delta_{11}$  and  $\Delta_{12}$ . Next, bisect each  $\Delta_{1i}$ ,  $i = 1, 2$ , forming four new triangles  $\Delta_{2i}$ ,  $i = 1, 2, 3, 4$ . Continue in this fashion. For every nonnegative integer  $n$ ,  $T_n = \{\Delta_{ni} : 1 \leq i \leq 2^n\}$ , so  $T_n$  is the set of  $2^n$  triangles created after the  $n$ -th iteration. Define  $m_n$ , the *mesh* of  $T_n$ , as the length of the longest side among the sides of all triangles in  $T_n$ . Also, let  $\gamma_n$  be the smallest angle among the angles of the triangles in  $T_n$ . We prove the following results:

- $\gamma_n = \min(\angle C, \angle A/2)$ , for all  $n \geq 1$ .
- $m_n \rightarrow 0$  as  $n \rightarrow \infty$ .
- Unless  $\Delta_{01}$  is an isosceles right triangle, the set  $\bigcup_{n=0}^{\infty} T_n$  contains infinitely many triangles no two of which are similar.

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