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Andrzej Dudek* (andrzej.dudek@wmich.edu), Western Michigan University, Department of Mathematics, Kalamazoo, MI 49024. *High powers of Hamiltonian cycles in randomly augmented graphs.*

We investigate the existence of powers of Hamiltonian cycles in graphs with large minimum degree to which some additional edges have been added in a random manner. It follows from the theorems of Dirac and of Komlós, Sárközy, and Szemerédi, who confirmed the Posá–Seymour conjecture, that for every $k \geq 1$ and sufficiently large n already the minimum degree $\delta(G) \geq \frac{k}{k+1}n$ for an n -vertex graph G alone suffices to ensure the existence of the k -th power of a Hamiltonian cycle. We show that under essentially the same degree assumption, i.e. for n -vertex graph G with minimum degree at least αn for any $\alpha > \frac{k}{k+1}$, with probability close to one, adding $O(n^{2-2/\ell})$ random edges yields the existence of the $(k\ell + r)$ -th power of a Hamiltonian cycle. Here, $k, \ell \geq 1, r \geq 0$ are integers satisfying $\ell \geq r(r + 1)$. We show that for several choices of k, ℓ , and r our result is asymptotically optimal.

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