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**Cédric Lecouvey** and **Cristian Lenart\*** (c.lenart@albany.edu), Department of Mathematics and Statistics, State University of New York at Albany, 1400 Washington Avenue, Albany, NY 12222. *Atomic decomposition of characters and crystals.*

Lusztig defined the Kostka-Foulkes polynomial  $K_{\lambda,\mu}(t)$  as a  $t$ -analogue of the multiplicity of a dominant weight  $\mu$  in the irreducible representation of highest weight  $\lambda$  of a semisimple Lie algebra. Lascoux stated that the type  $A$  Kostka-Foulkes polynomials expand positively in terms of so-called atomic polynomials. We define a combinatorial version of the atomic decomposition in arbitrary type, as a decomposition of a modified version of the Kashiwara crystal graph encoding the representation; this property can also be viewed as a strengthening of the monotonicity of  $K_{\lambda,\mu}(t)$ . We prove that the combinatorial atomic decomposition holds in type  $A$  (which provides a new, conceptual approach to Lascoux's statement), as well as in types  $B$ ,  $C$ , and  $D$  in a stable range for  $t = 1$ . We also give a geometric interpretation and other applications. (Received September 04, 2019)