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**Doğan Çömez\***, Minard 408, 1210 Albrecht Boulevard, Fargo, ND 58108, and **Mrinal Kanti Roychowdhury**. *Canonical sequences for the optimal quantization of condensation measures*. Preliminary report.

Let  $S_1(x) = cx$ ,  $S_2(x) = cx + r$ , for all  $x \in \mathbb{R}$ , where  $0 < c \leq \frac{1}{2}$  with  $c + r = 1$  and  $\nu$  be a Borel probability measure on  $\mathbb{R}$  with compact support. We consider condensation systems  $(\mathcal{S}, \mathbf{a}, \nu)$ , where  $\mathcal{S} = \{S_i\}_{i=1}^2$  are similarity maps and  $\mathbf{a} = (a_1, a_2, a_3)$  with  $a_1 + a_2 + a_3 = 1$ , with the associated condensation measure  $P := a_1 P \circ S_1^{-1} + a_2 P \circ S_2^{-1} + a_3 \nu$ . Let  $D(P)$  denote the quantization dimension of the measure  $P$ . We study self-similar measures  $\nu$  satisfying  $D(\nu) > \kappa$ ,  $D(\nu) < \kappa$ , and  $D(\nu) = \kappa$ , respectively, where  $\kappa = -\frac{\log 2}{\log c}$ . For particular cases of  $c, r$  and  $\mathbf{a}$ , we show that there exist sequences  $a(n)$  and  $F(n)$ , which are utilized to determine the optimal sets and associated quantization errors for the measure  $P$ . We also show that for each measure  $\nu$  the quantization dimension  $D(P)$  of the measure  $P$  exists and satisfies  $D(P) = \max\{\kappa, D(\nu)\}$ . It turns out that, for  $D(\nu) > \kappa$ , the  $D(P)$ -dimensional lower and upper quantization coefficients are finite, positive and unequal; and for  $D(\nu) \leq \kappa$ , the  $D(P)$ -dimensional lower quantization coefficient is infinity. (Received September 09, 2019)