In this talk I will describe the definition of constant slope families of $p$-adic modular forms through a fixed classical eigenform. We will then expose a result bounding their size. Our result is related to the $p$-adic arithmetic of the given eigenform through $L$-invariants and adjoint $p$-adic $L$-functions. (Received February 04, 2019)