Local and global pointwise gradient estimates are obtained for solutions to the quasilinear elliptic equation with measure data $-\text{div}(A(x, \nabla u)) = \mu$ in a bounded and possibly nonsmooth domain $\Omega$ in $\mathbb{R}^n$. Here $\text{div}(A(x, \nabla u))$ is modeled after the $p$-Laplacian. Our results extend earlier known results to the singular case in which $\frac{3n-2}{2n-1} < p \leq 2 - \frac{1}{n}$. (Received February 04, 2019)