In the talk we will discuss new developments of the theory of pullbacks of differential forms under Hölder continuous mappings with applications to the geometry and topology of the Heisenberg groups. In particular a new proof of the non-embedding theorem of Gromov and new results about Hölder homotopy groups of the Heisenberg groups will be discussed. (Received February 04, 2019)