We will talk about ancient solutions to the mean curvature flow in $\mathbb{R}^3$. In particular, we will concentrate on the solutions converging to the cylinder as $t \to -\infty$. In that case, we show the existence and the uniqueness of an ancient solution for each non-trivial eigenfunction. (Received February 03, 2019)