1153-05-41 **Mozhgan Mirzaei*** (momirzae@ucsd.edu) and **Andrew Suk**. *Extremal Configurations in Point-Line Arrangements.* Preliminary report.

The famous Szemerédi-Trotter theorem states that any arrangement of n points and n lines in the plane determines $O(n^{4/3})$ incidences, and this bound is tight. In this talk, we present some Turán-type results for point-line incidences. Let $\mathcal{L}_1$ and $\mathcal{L}_2$ be two sets of t lines in the plane and let $P = \{\ell_1 \cap \ell_2 : \ell_1 \in \mathcal{L}_1, \ell_2 \in \mathcal{L}_2\}$ be the set of intersection points between $\mathcal{L}_1$ and $\mathcal{L}_2$. We say that $(P, \mathcal{L}_1 \cup \mathcal{L}_2)$ forms a *natural* $t \times t$ *grid* if $|P| = t^2$, and $conv(P)$ does not contain the intersection point of some two lines in $\mathcal{L}_i$, for $i = 1, 2$. For fixed $t > 1$, we show that any arrangement of n points and n lines in the plane that does not contain a natural $t \times t$ grid determines $O(n^{\frac{4}{3}-\varepsilon})$ incidences, where $\varepsilon = \varepsilon(t)$. We also provide a construction of n points and n lines in the plane that does not contain a natural 2×2 grid and determines at least $\Omega(n^{1+\frac{1}{14}})$ incidences. Joint work with Andrew Suk. (Received August 08, 2019)