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**Sheldon Axler\*** ([axler@sfsu.edu](mailto:axler@sfsu.edu)). *Computing with Harmonic Functions.*

Fix a positive integer  $n$  and let  $B$  denote the open unit ball in  $\mathbf{R}^n$ .

- Dirichlet problem: Given  $f \in C(\partial B)$ , find the unique  $u \in C(\overline{B})$  such that  $u|_B$  is harmonic and  $u|_{\partial B} = f$ .
- Neumann problem: Given  $f \in C(\partial B)$  with mean value 0, find the unique  $u \in C(\overline{B})$  such that  $u|_B$  is harmonic, the outward normal derivative of  $u$  on  $\partial B$  equals  $f$ , and  $u(0) = 0$ .

Each of the two problems above has the perhaps unexpected property that if  $f$  is a polynomial of  $n$  variables, then  $u$  is a polynomial of  $n$  variables. This talk begins by focusing on the explicit computation in closed form of the linear map  $f \mapsto u$  given by each of the problems above. Then the ball is replaced by an ellipsoid, and new techniques are needed. (Received August 27, 2019)