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Mark Ellingham* (mark.ellingham@vanderbilt.edu), **Songling Shan, Dong Ye and Xiaoya Zha.** *Toughness and spanning trees in K_4 -minor-free graphs.*

For an integer k , a k -tree is a tree with maximum degree at most k . More generally, if f is an integer-valued function on vertices, an f -tree is a tree in which each vertex v has degree at most $f(v)$. Let $c(G)$ denote the number of components of a graph G . We investigate spanning trees in K_4 -minor-free graphs, which are identical to graphs of treewidth at most 2, and generalize series-parallel graphs. We show that if G is a connected K_4 -minor-free graph and

$$c(G - S) \leq \sum_{v \in S} (f(v) - 1) \quad \text{for all } S \subseteq V(G) \text{ with } S \neq \emptyset$$

then G has a spanning f -tree. Consequently, if G is a $\frac{1}{k-1}$ -tough K_4 -minor-free graph, then G has a spanning k -tree, which strengthens a result for general graphs due to Win. Examples show that this inequality cannot be relaxed by adding 1 to the right-hand side. (Received July 05, 2019)