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Yifan Jing, Alexandr Kostochka and Fuhong Ma\* (mafuhongsdnu@163.com), Shandong University, 27 Shanda Nanlu, Jinan, Shandong 250100, Peoples Rep of China, and Pongpat Sittitrai and Jingwei Xu. Defective DP-colorings of sparse multigraphs.

DP-coloring (also known as correspondence coloring) is a generalization of list coloring developed recently by Dvořák and Postle. We introduce and study defective DP-colorings of graphs and multigraphs with 2 colors. Each vertex v of a multigraph G has colors  $\alpha(v)$  and  $\beta(v)$  in its list. In an (i, j)-coloring of G, if v is colored with  $\alpha(v)$ , then it can be incident to at most i 'conflicting' edges, otherwise it can be incident to at most j such edges. We concentrate on (i, j)-colorings of sparse multigraphs.

Let  $f_{DP}(i, j, n)$  be the minimum number of edges that may have an *n*-vertex (i, j)-critical multigraph, that is, a multigraph G that has no (i, j)-defective DP-coloring but whose every proper subgraph has such a coloring. For all i and j, we find linear lower bounds on  $f_{DP}(i, j, n)$  that are exact for infinitely many n. (Received July 10, 2019)