Mikhalkin established the correspondence between holomorphic curves and tropical curves on toric surfaces. The result is generalized by Nishinou and Siebert and many others. Later, the tropical curves counting is getting interesting in mirror symmetry. Together with Travis Mandel, we develop to describe the counting in terms of quiver representations. (Received June 29, 2019)