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**Andrew B. Conner\*** (abc12@stmarys-ca.edu) and **Peter D. Goetz.** *Noncommutative Projective Geometry of Certain Twisted Tensor Products.* Preliminary report.

Let  $T = k\langle x_0, \dots, x_n \rangle$  denote the free associative  $k$ -algebra on generators of degree 1. Let  $A = T/I$  be the quotient by a finitely-generated, homogeneous ideal  $I$ . For  $d \geq 1$ , let  $Z_d \subset (\mathbb{P}^n)^{\times d}$  be the scheme of common zeros of elements of  $I_d$ , viewed as functions  $(T_1^*)^{\otimes d} \rightarrow k$ . From the geometric data of the schemes  $Z_d$ , one can define a ring structure on  $B = \bigoplus_d H^0(Z_d, i^* \mathcal{O}_{(\mathbb{P}^n)^{\times d}}(1))$  where  $i : Z_d \rightarrow (\mathbb{P}^n)^{\times d}$  is the inclusion.

If  $A$  is an Artin-Schelter (AS) regular algebra on three generators, then  $Z_d \cong Z_2$  for all  $d \geq 2$ , and  $Z_2$  is the graph of an automorphism  $\sigma$  on a scheme  $X$ . In this case,  $B$  is isomorphic to a twisted homogeneous coordinate ring on the data  $(X, \sigma, \mathcal{L})$  where  $\mathcal{L}$  is an invertible sheaf. If  $A$  is not AS-regular, the sequence  $\{Z_d\}$  need not stabilize.

In this talk we describe the schemes  $Z_d$  and the associated ring structure of  $B$  in the case where  $A$  is a quadratic twisted tensor product of  $k[x, y]$  and  $k[z]$ . Such twisted tensor products were recently classified by the authors, and the classification includes both AS-regular and non-noetherian examples. (Received March 02, 2020)