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Let $\mathbf{a} = (\mathbf{a}_1, \dots, \mathbf{a}_n)$ be a set of relatively prime positive integers minimally generating the numerical semigroup $\langle \mathbf{a} \rangle$. For every $1 \leq i \leq n$, there is a smallest positive integer c_i such that $c_i a_i = \sum_{j \neq i} a_j a_i$. Thus, there is an $n \times n$ matrix $D(\mathbf{a}) = (\mathbf{a}_{ij})_{n \times n}$ where the diagonal entries are $-c_i$. This is called a principal matrix of $D(\mathbf{a})$. Although $D(\mathbf{a})$ is not unique, certainly the diagonal entries of $D(\mathbf{a})$ are uniquely determined. The rank of $D(\mathbf{a}) \leq \mathbf{n} - \mathbf{1}$. When the rank of $D(\mathbf{a})$ is $n-1$, we can recover \mathbf{a} from it. We discuss the problem of characterizing the numerical semigroup when the rank is less than $n - 1$. In particular, we prove that the rank of $D(\mathbf{a}) \geq \mathbf{n}/\mathbf{2}$. This problem is intricate even when $n = 4$; we prove that when $n = 4$, the principal matrix will have rank 3 if it is not a gluing of two smaller numerical semigroups. We give examples to show that the converse is not true and why. (Received August 03, 2020)