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**James Farre\*** (`james.farre@yale.edu`). *Dense representations of discrete groups and bounded cohomology.*

Let  $\Gamma$  be a discrete group, and let  $\rho : \Gamma \rightarrow \text{Isom}^+(\mathbb{H}^3)$  be a homomorphism. We will define bounded cohomology  $H_b^\bullet(\Gamma)$  of  $\Gamma$  and describe an invariant of  $\rho$  in  $H_b^3(\Gamma)$  defined by computing the (signed) volumes of certain geodesic tetrahedra in  $\mathbb{H}^3$ . The main theorem is that this invariant is non-zero for representations with dense image. Moreover, if a dense representation exists, then the degree 3 bounded cohomology of  $\Gamma$  has uncountable dimension. Surprisingly, the proof relies on some non-trivial topology and geometry of 3-manifolds. The aim of the talk will be to explain how one can apply the ideas of the proof in dimension  $n \geq 4$ , given a hyperbolic  $n$ -manifold with some prescribed topological and geometric properties (if one exists). The discussion is already interesting when  $\Gamma$  is a non-abelian free group, in which case we do not know if bounded cohomology in degree larger than 3 is (non-)zero. (Received January 27, 2020)