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**Braden Balentine\*** ([braden.balentine@colorado.edu](mailto:braden.balentine@colorado.edu)), University of Colorado Boulder, Department of Mathematics, Campus Box 395, Boulder, CO 80302. *Well-Posedness and Global in Time Behavior for Mild Solutions to the Navier-Stokes Equation on the Hyperbolic Space with Initial Data in  $L^p$ .*

We discuss mild solutions to the Navier-Stokes equation on the  $n$ -dimensional hyperbolic space  $\mathbb{H}^n$ ,  $n \geq 2$ . Substantial results have been already obtained by Pierfelice. In this talk, we show how to extend the rest of the Fujita-Kato theory of mild solutions from  $\mathbb{R}^n$  to  $\mathbb{H}^n$ . This includes well-posedness results for  $L^p$  initial data in the range  $1 < p < \infty$ , global in time results for small initial data, and  $L^p$  norm decay results for both  $u$  and  $\nabla u$ . As part of this, we discuss extending to the hyperbolic space  $\mathbb{H}^n$  known facts in Euclidean space concerning the strong continuity and contractivity of the semigroup generated by the Laplacian. Also, we discuss necessary boundedness and commutation properties for a certain projection operator in the setting of  $\mathbb{H}^n$ . This work, together with Pierfelice's, contributes to providing a full theory for mild solutions on  $\mathbb{H}^n$ . (Received August 31, 2020)