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**Jeffrey Meier, Abigail Thompson and Alexander Zupan\*** (zupan@unl.edu). *Cubic graphs induced by bridge trisections.*

A bridge trisection of a knotted surface  $\mathcal{K} \subset S^4$  induces a cell decomposition of the underlying surface whose 1-skeleton is a cubic Tait-colored graph  $\Gamma$ ; that is, every vertex of  $\Gamma$  has valence three, and each edge of  $\Gamma$  is colored red, blue, or green, with the property that every vertex is incident to edges of all three colors. A natural question is whether this process can be reversed: Given a cubic Tait-colored graph  $\Gamma$ , does there exist a surface  $\mathcal{K} \subset S^4$  and a bridge trisection of  $\mathcal{K}$  inducing  $\Gamma$ ? We answer the question in the affirmative, showing further that  $\mathcal{K}$  can even be chosen to be unknotted and with any possible normal Euler number (if  $\mathcal{K}$  is nonorientable). (Received August 30, 2020)