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**Debarun Ghosh, Ervin Győri and Ryan R. Martin\***, Department of Mathematics, 428  
Carver Hall, Iowa State University, Ames, IA 50011, and **Addisu Paulos and Chuanqi Xiao**.

*Planar Turán number of the 6-Cycle.*

Let  $\text{ex}_{\mathcal{P}}(n, T, H)$  denote the maximum number of copies of  $T$  in an  $n$ -vertex planar graph which does not contain  $H$  as a subgraph. When  $T = K_2$ ,  $\text{ex}_{\mathcal{P}}(n, T, H)$  is the well studied function, the planar Turán number of  $H$ , denoted by  $\text{ex}_{\mathcal{P}}(n, H)$ . The topic of extremal planar graphs was initiated by Dowden (2016). He obtained sharp upper bound for both  $\text{ex}_{\mathcal{P}}(n, C_4)$  and  $\text{ex}_{\mathcal{P}}(n, C_5)$ . Later on, Y. Lan, et al. continued this topic and proved that  $\text{ex}_{\mathcal{P}}(n, C_6) \leq \frac{18(n-2)}{7}$ . In this paper, we give a sharp upper bound  $\text{ex}_{\mathcal{P}}(n, C_6) \leq \frac{5}{2}n - 7$ , for all  $n \geq 18$ , which improves Lan's result. We also pose a conjecture on  $\text{ex}_{\mathcal{P}}(n, C_k)$ , for  $k \geq 7$ . (Received August 10, 2020)