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General Famous Numbers: Stirling-Euler-Lah-Bell. Preliminary report.

We shall first introduce Pascal, Stirling, Eulerian, Lah and Bell numbers via sorting and generalize Stirling numbers of both kinds $S1(n,k)$, $S2(n,k)$, Eulerian numbers of two orders $E1(n,k)$, $E2(n,k)$, Lah numbers $L(n,k)$ and ordered Bell numbers $OB(a,d)$ from the natural number based to AP sequences based. There are two separate structures. 1) Stirling: $GS(n,k - A(i) - u;v)$ with $GS(1,1) = 1$ and $A(i)$ is an arbitrary infinite sequence, u and v are numbers, each indicating which weight to be used among $SW(1)=1$, $SW(2)=A(n-1)$, $SW(3)=A(k)$ and $SW(4)=A(n+k)-1$ in $GS(n,k)=SW(u)GS(n-1,k-1)+SW(v)GS(n-1,k)$; 2) Euler: $GE(n,k - A(i) - u;v)$, with $GE(1,0) = 1$, where u , v each indicating which weight to be used among $EW(1)=A(n-1)$, $EW(2)=A(k)$ and $EW(3)=A(n-k)$ in $GE(n,k)=EW(u)GE(n-1,k-1)+EW(v)GE(n-1,k)$. Therefore, $S1ad(n,k)=GS(n, k - A(i)=a+(i-1)d - 1;2)$, $S2ad(n,k)=GS(n, k - A(i)=a+(i-1)d - 1;3)$, $E1ad(n,k)=GE(n, k - A(i)=a+(i-1)d - 1;2)$, $E2ad(n,k)=GE(n, k - A(i)=a+(i-1)d - 3;2)$, $Lad(n,k)=GS(n, k - A(i)=a+(i-1)d - 1;4)$. Moreover, a peculiar formula involving Stirling, Eulerian and ordered Bell numbers is generalized from the natural number based to AP sequences based and as well. (Received December 22, 2020)