Susan Cooper, Sabine El Khoury, Sara Faridi, Sarah Mayes-Tang and Susan Morey*, Department of Mathematics, Texas State University, 601 University Dr., San Marcos, TX 78666, and Liana Sega and Sandra Spiroff. Polyhedral Resolutions of Powers of Monomial Ideals of Projective Dimension One.

Using combinatorial structures to obtain resolutions of monomial ideals traces back to Diana Taylor's thesis, where a simplex associated to the generators of a monomial ideal was used to construct a free resolution of the ideal. This concept has been expanded, with various authors determining conditions under which simplicial or cellular complexes can be associated to monomial ideals to produce a free resolution. This talk will focus on powers of square-free monomial ideals of projective dimension one. Faridi and Hersey proved that a monomial ideal I has projective dimension one if and only if there is an associated tree T that supports a free resolution of I. Using a quotient of a standard graph product, we construct from this tree a set of graphs T^r . By iteratively appending cells of increasing dimensions, these graphs can be viewed as the one-skeleta of polyhedral complexes that resolve the powers I^r of I. Moreover, each of these resolutions will be minimal resolutions. These cellular resolutions can also be viewed as strands of the resolution of the Rees algebra of I. This work is part of a research project initiated at a BIRS workshop "Women in Commutative Algebra" in Fall 2019 where the authors studied resolutions of powers of monomial ideals. (Received February 26, 2021)