

1172-11-216

Thomas Grubb* (tgrubb@ucsd.edu), **Kiran Kedlaya** (kedlaya@ucsd.edu) and **James Upton** (jtupton@ucsd.edu). *A cut-by-curves criterion for overconvergence of F -isocrystals*. Preliminary report.

Let X be a smooth, geometrically irreducible scheme over a finite field of characteristic $p > 0$. With respect to rigid cohomology, p -adic coefficient objects on X come in two types: convergent F -isocrystals and the subcategory of overconvergent F -isocrystals. Overconvergent isocrystals are related to ℓ -adic étale objects ($\ell \neq p$) via companions theory, and as such it is desirable to understand when an isocrystal is overconvergent. We show (under a geometric tameness hypothesis) that a convergent F -isocrystal \mathcal{E} is overconvergent if and only if its restriction to all smooth curves on X is. The technique reduces to an algebraic setting where we use skeleton sheaves and crystalline companions to compare \mathcal{E} to an isocrystal which is patently overconvergent. Joint with Kiran Kedlaya and James Upton. (Received August 29, 2021)