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**Shanna Dobson\***, Shanna.Dobson@calstatela.edu.  $(\infty, 1)$ -Grothendieck Construction of Spatial Diamonds and  $V$ -Stacks. Preliminary report.

Motivated by Scholze's étale cohomology of diamonds and Scholze and Fargues' geometrization of the local Langlands correspondence, we conjecture a universal construction of spatial diamonds. We then extend this universal construction to an  $(\infty, 1)$ -Grothendieck construction on our  $(\infty, 1)$ -category of spatial diamonds. A diamond  $\mathcal{D}$  is a certain pro-étale sheaf on the category of perfectoid spaces of characteristic  $p$ . A perfectoid space is an adic space covered by adic spaces of the form  $\mathrm{Spa}(R, R^+)$  for  $R$  a perfectoid ring. A spatial diamond is a small  $v$ -sheaf in the  $v$ -topology, which is a Grothendieck topology. Constructing quotients of diamonds by a diamond equivalence relation yields  $v$ -sheaves and constructing quotients of small  $v$ -sheaves by a small  $v$ -sheaf equivalence relation produces  $v$ -stacks. We conclude by discussing a universal construction of  $v$ -stacks. (Received July 10, 2021)