

1173-00-237

**Alisina Azhang\*** (aazhan1@lsu.edu), 3033 July St. Apt.210, Baton Rouge, LA 70808. *Rigid Connections on the Projective Line with Elliptic Toral Singularities*. Preliminary report.

We generalize two studies of rigid  $G$ -connections on  $\mathbb{P}^1$  which have an irregular singularity at origin and a regular singularity at infinity with unipotent monodromy: one is the work of Kamgarpour-Sage which classifies rigid homogeneous Coxeter  $G$ -connections with slope  $\frac{r}{h}$ , where  $h$  is the Coxeter number of  $G$ , and the other is the work of Chen, which proves the existence of rigid homogeneous elliptic regular  $G$ -connections with slope  $\frac{1}{m}$ , where  $m$  is an elliptic number for  $G$ . In our work, similar to Chen, we look for rigid homogeneous elliptic regular  $G$ -connections, but we allow the slope to have a numerator greater than 1. However, for the present purpose, we essentially restrict to the case where  $G$  is either  $\mathrm{Sp}_{2n}$  or  $\mathrm{SO}_{2n+1}$ . For  $\mathrm{Sp}_{2n}$ , we show that Kamgarpour-Sage connections and Chen connections exhaust all the rigid homogeneous elliptic regular connections. For  $\mathrm{SO}_{2n+1}$ -connections, having introduced the notion of "generalized Chen connections," we classify all rigid connections of this type. We conjecture that any rigid homogeneous elliptic regular  $\mathrm{SO}_{2n+1}$ -connection is in this form. (Received September 21, 2021)