

1173-05-316

**Matt Superdock\*** ([superdockm@rhodes.edu](mailto:superdockm@rhodes.edu)). *Simplicial complexes, finite projective planes, and colored configurations.*

In the 7-vertex triangulation of the torus, the 14 triangles can be partitioned as  $T_1 \sqcup T_2$ , such that each  $T_i$  represents the lines of a copy of the Fano plane  $PG(2, \mathbb{F}_2)$ . We generalize this observation by constructing, for each prime power  $q$ , a simplicial complex  $K$  with  $q^2 + q + 1$  vertices and  $2(q^2 + q + 1)$  facets consisting of two copies of  $PG(2, \mathbb{F}_q)$ .

Our construction works for any *colored  $k$ -configuration*, defined as a  $k$ -configuration whose associated bipartite graph  $G$  is connected and has a  $k$ -edge coloring  $\chi: E(G) \rightarrow [k]$ , such that for all  $v \in V(G)$ ,  $a, b, c \in [k]$ , following edges of colors  $a, b, c, a, b, c$  from  $v$  brings us back to  $v$ . We give constructions of colored  $k$ -configurations from planar difference sets and commutative semifields. Then we give one-to-one correspondences between (1) Sidon sets of order 2 and size  $k + 1$  in groups with order  $n$ , (2) linear codes with radius 1 and index  $n$  in  $A_k$ , and (3) colored  $(k + 1)$ -configurations with  $n$  points and  $n$  lines. (Received September 21, 2021)