Hal Schenck, Mike Stillman and Beihui Yuan\* (by238@cornell.edu). Calabi-Yau threefolds in projective spaces and Gorenstein rings.

A projectively normal Calabi-Yau threefold X in projective spaces has an ideal  $I_X$  which is arithmetically Gorenstein, of Castelnuovo-Mumford regularity four. Such ideals have been intensively studied when  $I_X$  is a complete intersection, as well as in the case where X is codimension three. In the latter case, the Buchsbaum-Eisenbud theorem shows that  $I_X$  is given by the Pfaffians of a skew-symmetric matrix. A number of recent papers study the situation when  $I_X$  has codimension four. We prove there are 16 possible Betti diagrams for an arithmetically Gorenstein ideal I with codim(I) = 4 = reg(I), and that exactly 8 of these occur for smooth irreducible nondegenerate threefolds. (Received September 16, 2021)