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We analyse positive solutions  $(u, v)$  to the steady state reaction diffusion system:

$$\begin{cases} -\Delta u = \lambda u(1 - u); \Omega \\ -\Delta v = \lambda r v(1 - v); \Omega \\ \frac{\partial u}{\partial \eta} + \sqrt{\lambda} g(v) u = 0; \partial \Omega \\ \frac{\partial v}{\partial \eta} + \sqrt{\lambda} h(u) v = 0; \partial \Omega \end{cases}$$

where  $\lambda > 0$ ,  $r > 0$  are parameters and  $g, h \in C^1([0, \infty), (0, \infty))$  are decreasing functions. This system models the steady states of two species living in a habitat where the interaction is limited to the boundary. Here,  $\lambda$  is directly proportional to the size of the habitat and we will study the ranges of  $\lambda$  where coexistence and nonexistence occurs. Namely, we will consider three cases: (a)  $E_1(1, g(0)) = E_1(r, h(0))$ , (b)  $E_1(1, g(0)) > E_1(r, h(0))$ , (c)  $E_1(1, g(0)) < E_1(r, h(0))$ . Here  $E_1(r, K)$  denotes the principal eigenvalue of:  $-\Delta z = r E z; \Omega, \frac{\partial z}{\partial \eta} + K \sqrt{E} z = 0; \partial \Omega$  (Received September 21, 2021)