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We consider an inverse diffusion problem: Given  $\phi$ , find  $\kappa$  such that  $\nabla \cdot (\kappa \nabla \phi) = 0$ . Stable variational formulations exist for this problem treated as a first-order hyperbolic system for  $\kappa$  [?, ?]. The smoothness requirements for these approaches are overly restrictive, however, and are ill-suited to the inverse problem. We present a new mixed variational formulation for the inverse diffusion problem that allows the solution and derivatives of the data to be in  $L(\Omega)$ . The formulation is a quadratic optimization problem based on minimizing the error in constitutive equations, and can be solved directly (ie. without iterations) for the unknown parameters. We prove that this formulation is well-posed for inverse diffusion with mild conditions on the data. We show through computational examples that a stabilized Galerkin discretization converges with mesh refinement. Finally, we extend the formulation to inverse elasticity and show promising computational results in this system. (Received January 21, 2022)