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**Matthias Franz\*** (mfranz@uwo.ca). *The Chang-Skjelbred lemma.*

Let  $T \cong (S^1)^r$  be a torus and  $X$  a sufficiently nice  $T$ -space, for example a compact  $T$ -manifold or a complex algebraic variety with an action of the complexification  $(\mathbb{C}^\times)^r$  of  $T$ . Assume that the equivariant cohomology  $H_T^*(X)$  of  $X$  with real coefficients is free over the polynomial ring  $H^*(BT)$ . The Chang-Skjelbred lemma asserts that the Chang-Skjelbred sequence

$$0 \longrightarrow H_T^*(X) \longrightarrow H_T^*(X^T) \longrightarrow H_T^{*+1}(X_1, X^T)$$

is exact in this case, where  $X^T$  denotes the  $T$ -fixed points and  $X_1$  the orbits of dimension at most 1. This allows to compute  $H_T^*(X)$ , including the ring structure, from  $X^T$  and  $X_1$  alone. In the case where the equivariant 1-skeleton  $X_1$  consists of finitely many 2-spheres, glued together at their poles, this approach has been popularized by Goresky–Kottwitz–MacPherson and is therefore often called the GKM method.

In this expository talk I will discuss these powerful results together with several examples. I will also survey various extensions: to other groups, to other coefficients and to spaces with non-free equivariant cohomology. (Received January 25, 2022)