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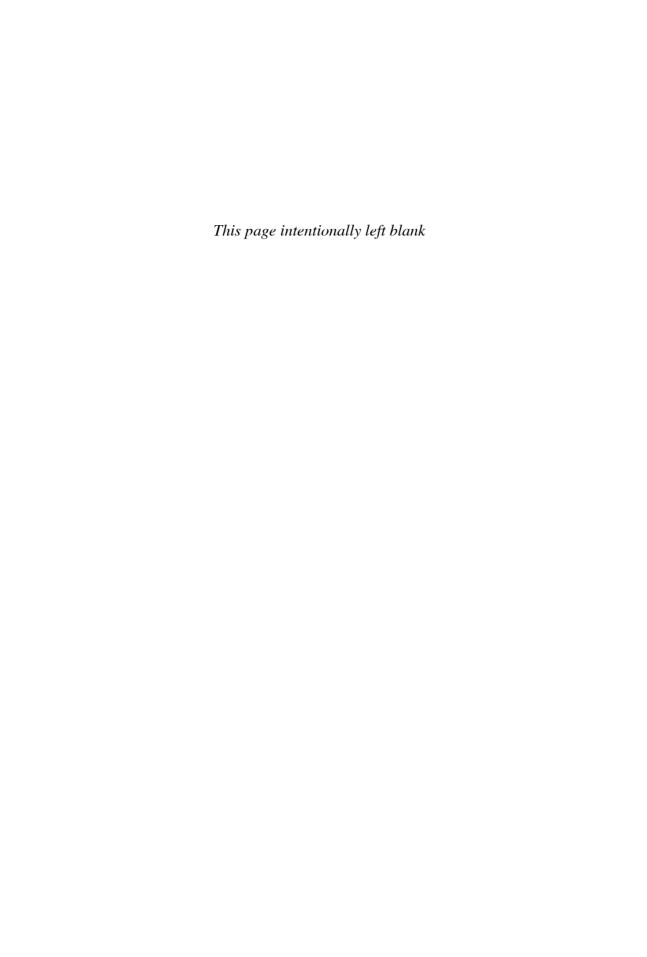




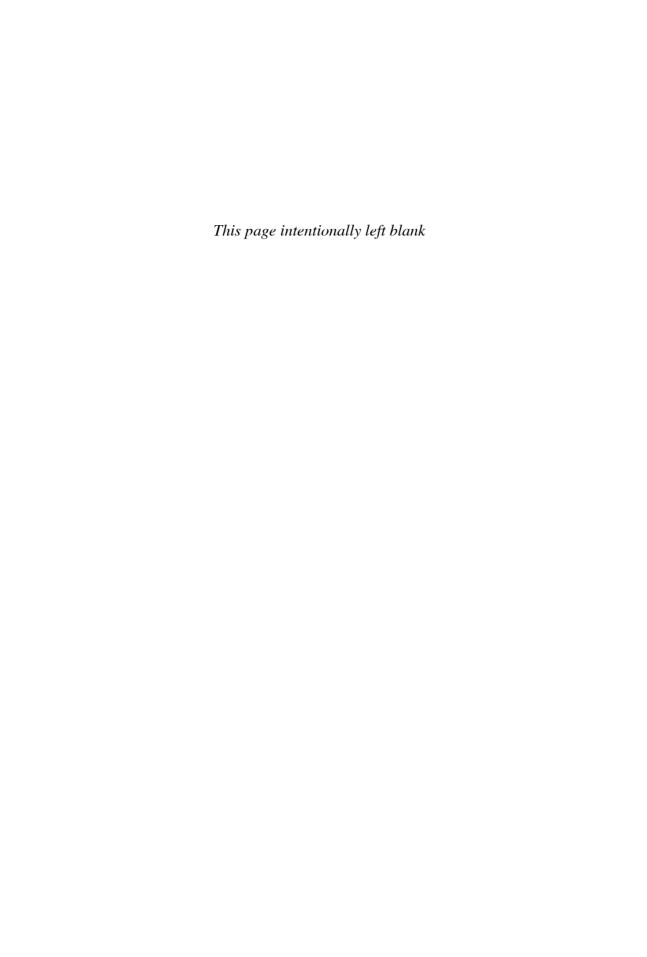
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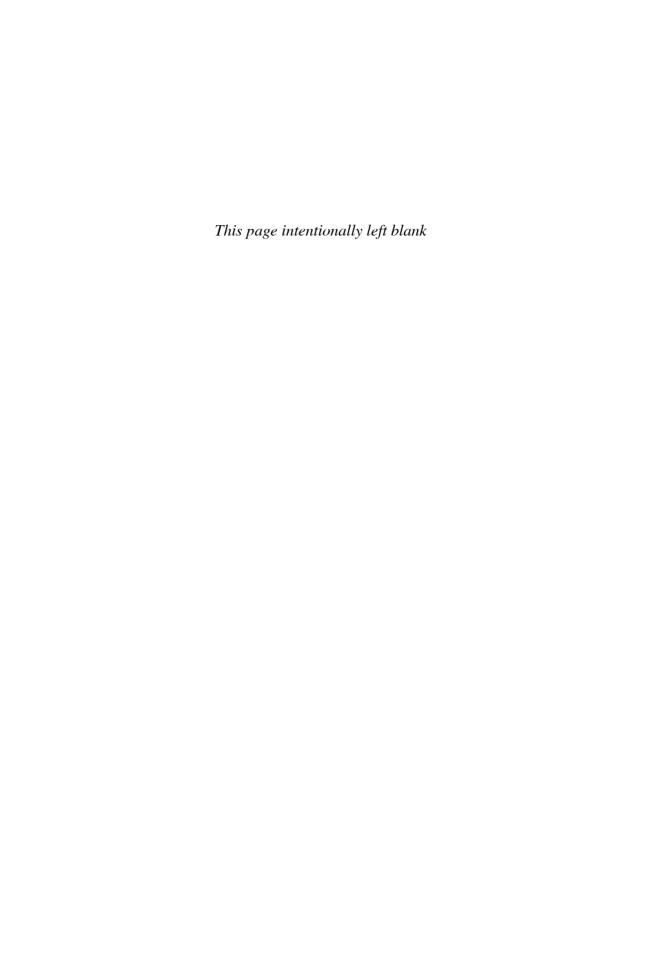
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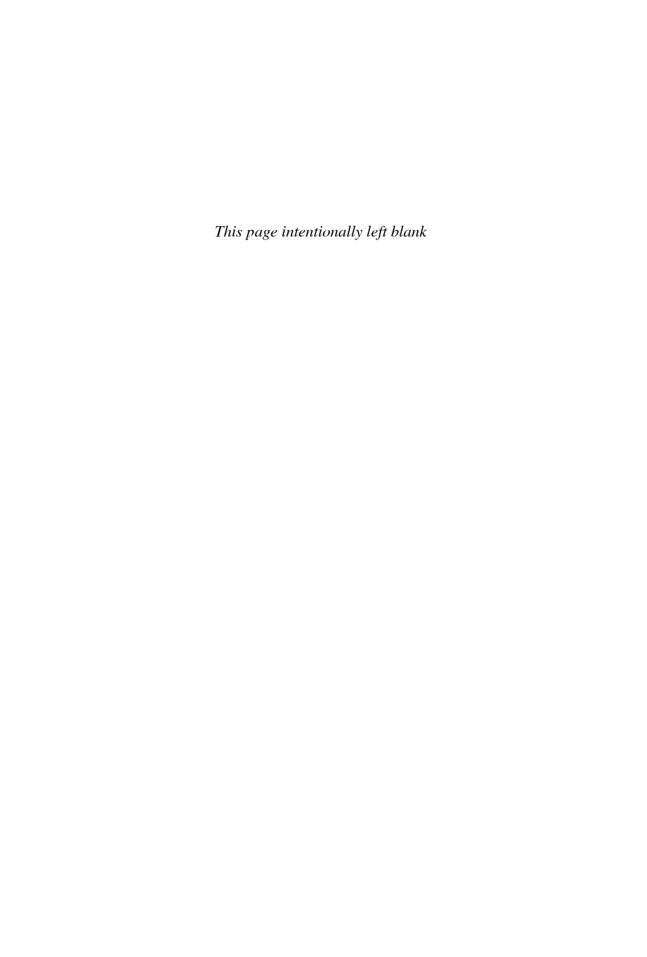
Tight closure began in a conversation with Mel Hochster at a conference at the University of Illinois in November of 1986. Serious work on tight closure began early in 1987, and the subject quickly took flight. Without Mel Hochster the topic of this manuscript would not exist, and these notes are a tribute to his beautiful ideas and immense contributions.

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Craig Huneke, August, 1995



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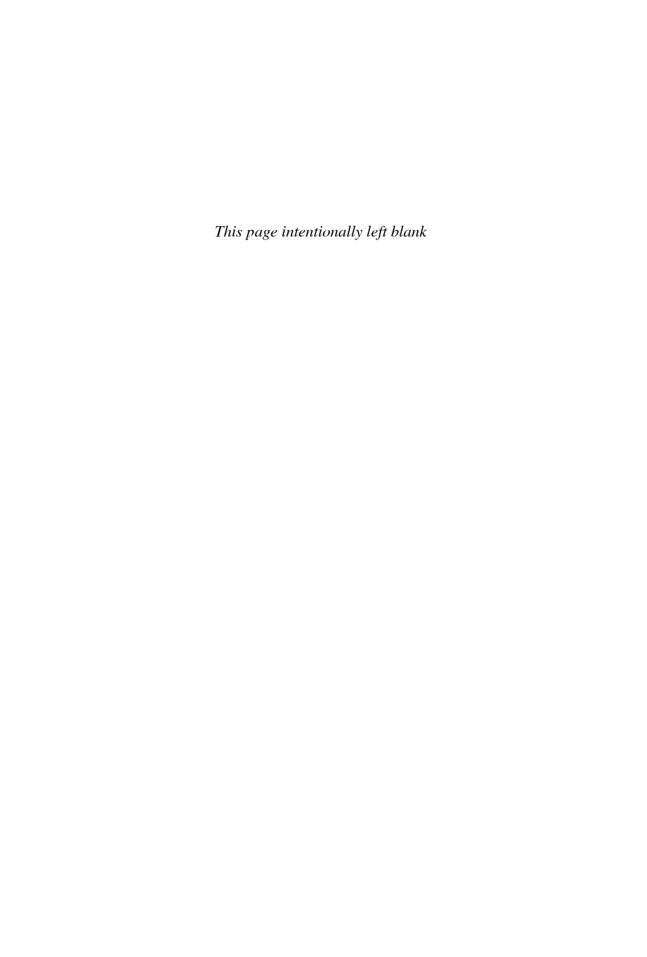
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