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Residues and Traces of Differential Forms via Hochschild Homology

Joseph Lipman

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via Hochschild Homology**

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1980 *Mathematics Subject Classification*. Primary 13D99, 14F10, 16A61, 32A27.

Library of Congress Cataloging-in-Publication Data

Lipman, Joseph

Residues and traces of differential forms via Hochschild homology

(Contemporary mathematics, ISSN 0271-4132; v. 61)

Bibliography: p.

1. Congruences and residues. 2. Homology theory. I. Title. II. Title: Hochschild homology.

III. Series.

QA244.L49 1987

512'.72

86-28698

ISBN 0-8218-5070-9 (alk. paper)

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CONTENTS

§0 Introduction	1
§1 The residue homomorphism	7
§2 Functorial properties.....	26
§3 Quasi-regular sequences	43
Appendix A: Residues on algebraic varieties	56
Appendix B: Exterior differentiation	63
§4 Trace and cotrace	68
References	95

ISBN 978-0-8218-5070-1



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CONM/61