Residues and Traces of Differential Forms via Hochschild Homology

Joseph Lipman
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Residues and Traces of Differential Forms via Hochschild Homology
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Joseph Lipman
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