

CONTEMPORARY MATHEMATICS

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111

Finite Geometries and Combinatorial Designs

Proceedings of the AMS Special Session in Finite Geometries and Combinatorial Designs held October 29–November 1, 1987

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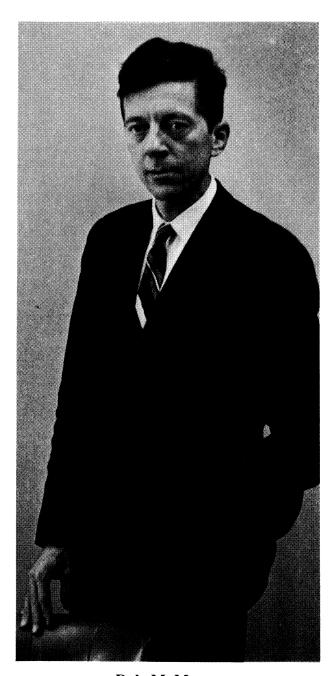
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Finite Geometries and Combinatorial Designs



Dale M. Mesner



CONTEMPORARY MATHEMATICS

111

Finite Geometries and Combinatorial Designs

Proceedings of the AMS Special Session in Finite Geometries and Combinatorial Designs held October 29–November 1, 1987

Earl S. Kramer and Spyros S. Magliveras, Editors

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The AMS Special Session in Finite Geometries and Combinatorial Designs was held at the University of Nebraska, Lincoln, Nebraska, October 29-November 1, 1987.

1980 Mathematics Subject Classification (1985 Revision). Primary 05BXX, 51EXX.

Library of Congress Cataloging-in-Publication Data

Finite geometries and combinatorial designs: proceedings of the AMS Special Session in Finite Geometries and Combinatorial Designs held October 29-November 1, 1987 [Lincoln, Nebraska]/Earl S. Kramer and Spyros S. Magliveras, editors.

p. cm.—(Contemporary mathematics, ISSN 0271-4132; v. 111) Includes bibliographical references. ISBN 0-8218-5118-7

1. Finite geometries—Congresses. 2. Combinatorial designs and configurations—Congresses. I. Kramer, Earl S. (Earl Sidney), 1940-. II. Magliveras, Spyros S. (Spyros Simos), 1938-. III. Title. IV. Series: Contemporary mathematics (American Mathematical Society); v. 111. QA167.2.A47 1987

515'.13—dc20

90-45302 CIP

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This volume was prepared by the authors using AMS-T_FX, the American Mathematical Society's TEX macro system.

> 10987654321 95 94 93 92 91 90

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DALE M. MESNER

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Preface

A special session on Finite Geometries and Combinatorial Designs was held at a regional conference of the American Mathematical Society in Lincoln, Nebraska during October 29-November 1, 1987. The organizers of the session were Dale Mesner and the editors of these proceedings. We were pleasantly surprised at the large number of participants from several countries who came to Lincoln for the three-day conference. We were even more pleased at the very high quality of results presented at the conference and submitted to the proceedings. We wish to thank conference participants, contributors to this volume, and referees. The editors take the liberty of dedicating this volume to Dale M. Mesner in appreciation of his contributions to combinatorics.

The editors express their thanks to the University of Nebraska, especially the Department of Computer Science and the Department of Mathematics, for funding and other support. Very special gratitude is due to Leanne Magliveras for her expert typesetting of the manuscripts.

Spyros S. Magliveras Earl S. Kramer Lincoln, Nebraska November, 1989

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ISBN 0-8218-5118-7