CONTEMPORARY MATHEMATICS

430

Ergodic Theory and Related Fields

2004–2006 Chapel Hill Workshops on Probability and Ergodic Theory University of North Carolina Chapel Hill, North Carolina

> Idris Assani Editor



American Mathematical Society

CONTEMPORARY MATHEMATICS

430

Ergodic Theory and Related Fields

2004–2006 Chapel Hill Workshops on Probability and Ergodic Theory University of North Carolina Chapel Hill, North Carolina

> Idris Assani Editor



American Mathematical Society Providence, Rhode Island

Editorial Board

Dennis DeTurck, managing editor

George Andrews Andreas Blass Abel Klein

2000 Mathematics Subject Classification. Primary 28D05, 37A05, 37A20, 37A50, 47A35, 47A16, 60F15, 82C20, 60G50.

Library of Congress Cataloging-in-Publication Data

Chapel Hill Ergodic Theory Workshop. Ergodic theory and related fields : 2004-2006 Chapel Hill Workshops on Probability and Ergodic Theory / Idris Assani, editor. p. cm. Includes bibliographical references. ISBN-13: 978-0-8218-3869-3 (alk. paper) ISBN-10: 0-8218-3869-5 (alk. paper)
1. Ergodic theory—Congresses. I. Assani, Idris. II. Title.

QA313.C43 2007 515'.48—dc22

2007060037

Copying and reprinting. Material in this book may be reproduced by any means for educational and scientific purposes without fee or permission with the exception of reproduction by services that collect fees for delivery of documents and provided that the customary acknowledgment of the source is given. This consent does not extend to other kinds of copying for general distribution, for advertising or promotional purposes, or for resale. Requests for permission for commercial use of material should be addressed to the Acquisitions Department, American Mathematical Society, 201 Charles Street, Providence, Rhode Island 02904-2294, USA. Requests can also be made by e-mail to reprint-permission@ams.org.

Excluded from these provisions is material in articles for which the author holds copyright. In such cases, requests for permission to use or reprint should be addressed directly to the author(s). (Copyright ownership is indicated in the notice in the lower right-hand corner of the first page of each article.)

© 2007 by the American Mathematical Society. All rights reserved.

The American Mathematical Society retains all rights

except those granted to the United States Government.

Copyright of individual articles may revert to the public domain 28 years

after publication. Contact the AMS for copyright status of individual articles. Printed in the United States of America.

I finited in the Onited States of America.

 \otimes The paper used in this book is acid-free and falls within the guidelines established to ensure permanence and durability.

Visit the AMS home page at http://www.ams.org/

10 9 8 7 6 5 4 3 2 1 12 11 10 09 08 07

Contents

Preface	v
Averages along cubes for not necessarily commuting m.p.t. IDRIS ASSANI	1
On the one-sided ergodic Hilbert transform IDRIS ASSANI and MICHAEL LIN	21
Concepts behind divergent ergodic averages along the squares ZOLTÁN BUCZOLICH and R. DANIEL MAULDIN	41
Deterministic walks in Markov environments with constant rigidity LEONID A. BUNIMOVICH and ALEX YURCHENKO	57
On random Fourier-Stieltjes transforms GUY COHEN	73
Limit theorems for sequential expanding dynamical systems on $[0, 1]$ JEAN-PIERRE CONZE and ALBERT RAUGI	89
$\{m_n\}$ -odometer and the binary odometer are finitarily orbit equivalent MRINAL KANTI ROYCHOWDHURY	123
Some open problems IDRIS ASSANI	135

Preface

The present volume contains contributions from participants to the 2004-2005 and 2006 Chapel Hill Ergodic Theory Workshops. These workshops were held in February 2004, 2005, and 2006 at Chapel Hill. They started in the summer of 2002 and now are a recurrent event. The 2007 workshop is scheduled for February 15-18, 2007. The list of participants outside Chapel Hill for these 2004-2006 workshops is the following: 2004: Zoltan Buczolich (Eötvös University - Hungary), Jean-Pierre Conze (University of Rennes1 - France), Christophe Cuny* (Ben- Gurion University, Israel), Geoffrey Goodson (Towson University), Nikos Frantzikinakis* (Penn State University), Ted Hill (Georgia Institute of Technology), Fern Hunt (National Institute of Standards and Technology), Michael Keane (Wesleyan University), Michael Lin (Ben-Gurion University, Israel), Jonathan C. Mattingly** (Duke University), Daniel Mauldin (University of North Texas), and Arkady Tempelman (Penn State University).

2005: Leonid Bunimovich (Georgia Institute of Technology), Mrinal Roychowdhury* (Wesleyan University), Miaohua Jiang (Wake Forest University), Michael Lin (Ben-Gurion University, Israel), William Massey (Princeton University), Arlie O. Petters (Duke University), and Kimberly Weems** (NC State University).

2006: Zoltan Buczolich (Eötvös University - Hungary), Alexander Bufetov* (University of Chicago), Guy Cohen* (Hebrew University of Jerusalem), Jean-Pierre Conze (University of Rennes1 - France), Rudy Horne* (University of Florida), Michael Lin (Ben-Gurion University, Israel), Jason Lucier* (Cent. Rech. Math.-Montreal), Daniel Mauldin (University of North Texas), Mrinal Roychowdhury* (Colorado State University), Ilya Shkredov**(Moscow State University), and Christoph Thiele (UCLA).

The participants' names with asterisks were younger researchers (graduate students, post-doctoral students or assistant professors**) at that time. The talks given by these outside participants covered a large range of topics in ergodic theory and related fields that include probability theory, combinatorics and harmonic analysis. A complete list of participants with the UNC senior and young researchers can be seen at the workshops' web sites: www.unc.edu/~assani/ErgWork04/, www.unc.edu/~assani/ErgWork05 and www.unc.edu/~assani/ErgWork06. Some open problems presented and discussed during the workshops are listed at the end of the volume.

It is a pleasure to acknowledge the institutions whose support made these events possible. First we thank the National Science Foundation and the Mathematical Sciences Research Institute at Berkeley for their continued support. Thanks also to the Department of Mathematics, the Deans of the College of Arts and Sciences and the Vice Chancellor for research at the University of North Carolina at Chapel Hill for their support. We have appreciated the energetic support of the staff and interested graduate students in the Department of Mathematics.

Finally we appreciate the support of the American Mathematical Society and its Contemporary Mathematics staff. A special thanks to Christine Thivierge for her guidance throughout the publication process. The book contains papers by participants of the Chapel Hill Ergodic Theory Workshops organized in February 2004, 2005, and 2006. Topics covered by these papers illustrate the interaction between ergodic theory and related fields such as harmonic analysis, number theory, and probability theory.



