# CONTEMPORARY MATHEMATICS

523

## Error-Correcting Codes, Finite Geometries and Cryptography

Conference on Error-Control Codes, Information Theory and Applied Cryptography December 5–6, 2007 Fields Institute, Toronto, Ontario, Canada

Canadian Mathematical Society Special Session Error Control Codes, Information Theory and Applied Cryptography CMS Winter Meeting December 8–10, 2007 London, Ontario, Canada

Aiden A. Bruen, David L. Wehlau Editors



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This volume contains the proceedings of two conferences on Error-control Codes, Information Theory and Applied Cryptography. The first was held at the Fields Institute, Toronto, ON, Canada, from December 5-6, 2007, and the second was a Canadian Mathematical Society Special Session at the CMS Winter Meeting, London, ON, Canada, from December 8-10, 2007.

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#### **Preface**

In December 2007 two back-to-back interdisciplinary conferences on Error Correcting Codes, Information Theory and Applied Cryptography took place. The first one was held at the Fields Institute in Toronto. The follow-up was in the format of a "Special Session" at the Winter Meeting of the Canadian Mathematical Society in London, Ontario. The organizers, in each case, were the Editors of this Volume. The Editors were very pleased by the large number of distinguished participants from several countries who journeyed to Ontario for these conferences. We were also gratified by the high quality of the results that were presented. This Volume is an outgrowth of the two meetings. It features contributions both from participants and from authors who, for one reason or another, had not been able to attend. The interdisciplinary nature can best be understood from a perusal of the table of contents. The papers are split within the areas of Cryptography, Finite Geometries and Error-Control Codes. Several of the papers could easily fit in two, or even all three, of these categories. It becomes ever more difficult to affect a separation of the areas. In fact we are convinced that the future of the three areas lies in an interdisciplinary approach and in a common treatment wherever possible.

The Cryptography section features papers in "classical" topics such as hash functions, privacy amplification and key distribution as well as the latest on "Quantum Coins". In Finite Geometries there are contributions about nets, partial spreads, geometric incidence matrices, Andre embeddings along with geometric configurations, planar representations, partial spreads and families of mutually orthogonal latin squares.

The largest section deals with codes in one form or another. The hardy perennials of MDS codes, such as Reed-Solomon and LDPC codes are well represented as well as perfect codes, orthogonal codes and quantum codes. There is a paper on classical linear codes and their duals. The *p*-ranks for designs are studied. In communication theory we have papers on iterative and concatenated codes and on communications over a random-access channel. Another paper deals with recent work on very applied topics relating to magnetic data-storage systems

We would be remiss were we not to acknowledge the gracious hospitality of the Fields Institute and Massey College in the University of Toronto. We also thank Professor Carl Riehm of the Fields Institute together with Gertrud Jeewanjee and the staff at the Canadian Mathematical Society.

Aiden A Bruen, University of Calgary

David L. Wehlau, Royal Military College of Canada February 2010

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This interdisciplinary volume contains papers from both a conference and special session on Error-Control Codes, Information Theory and Applied Cryptography. The conference was held at the Fields Institute in Toronto, ON, Canada from December 5–6, 2007, and the special session was held at the Canadian Mathematical Society's winter meeting in London, ON, Canada from December 8–10, 2007.

The volume features cutting-edge theoretical results on the Reed–Muller and Reed–Solomon codes, classical linear codes, codes from nets and block designs, LDPC codes, perfect quantum and orthogonal codes, iterative decoding, magnetic storage and digital memory devices, and MIMO channels. There are new contributions on privacy reconciliation, resilient functions, cryptographic hash functions, and new work on quantum coins. Related original work in finite geometries concerns two-weight codes coming from partial spreads, (0,1) matrices with forbidden configurations, André embeddings, and representations of projective spaces in affine planes.

Great care has been taken to ensure that high expository standards are met by the papers in this volume. Accordingly, the papers are written in a user-friendly format. The hope is that this volume will be of interest and of benefit both to the experienced and to newcomers alike.



