# **CONTEMPORARY MATHEMATICS**

### 536

## Cross Disciplinary Advances in Quantum Computing

NSF Sponsored Research Conference on Representation Theory, Quantum Field Theory, Category Theory, and Quantum Information Theory October 1–4, 2009 University of Texas at Tyler Tyler, Texas

> Kazem Mahdavi Deborah Koslover Leonard L. Brown III Editors



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2000 Mathematics Subject Classification. Primary 81P68, 81-01, 81-02, 81-06.

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#### Library of Congress Cataloging-in-Publication Data

Conference on Representation Theory (2009 : University of Texas at Tyler)

Cross disciplinary advances in quantum computing : Conference on Representation Theory, Quantum Field Theory, Category Theory, and Quantum Information Theory, October 1–4, 2009, University of Texas at Tyler, Tyler, Texas / Kazem Mahdavi, Deborah Koslover, Leonard L. Brown, III, editors.

p. cm. — (Contemporary mathematics; v. 536)

Includes bibliographical references.

ISBN 978-0-8218-4975-0 (alk. paper)

1. Quantum theory—Mathematics—Congresses. 2. Quantum communication—Congresses. I. Mahdavi, Kazem. II. Koslover, Deborah. III. Brown, Leonard L., 1972– IV. Title.

QC174.17.M35C66 2009 530.12—dc22

2010045181

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#### Preface

Building on the success of the 2007 conference, the 2009 Conference on Representation Theory, Quantum Field Theory, Category Theory, and Quantum Information Theory, was held October 1–4 at the University of Texas at Tyler. It was funded by the NSF for the purpose of bringing together scientists from a wide range of fields to share research and stimulate new ideas. Attendees included mathematicians, physicists, and computer scientists. Speakers came from major industries including IBM; major national laboratories including the Army Research Lab, Air Force Office of Scientific Research, Los Alamos and Argonne National Lab; and major education institutions including Harvard, Oxford, and Moscow State University.

Our main purpose in publishing this proceedings volume is to bring together papers from a wide spectrum of disciplines to stimulate progress in the field of computation and communication, in particular, quantum communication (QC). The seven contributed papers included in this volume cover a wide range of topics related to QC, including physical aspects, mathematical aspects and foundational issues of QC. All submissions were peer reviewed and the most outstanding have been chosen to appear here.

As a general rule, every book is written with the goal of expanding the horizon of human knowledge. We hope this volume will lead to advances in QC.

The editors would like to thank our co-organizers, Louis Kauffman (UIC) and Samuel Lomonaco (UMBC), of the Conference on Representation Theory, Quantum Field Theory, Category Theory, and Quantum Information Theory.

We would also like to thank our wonderful speakers: Samson Abramsky (Oxford), Paul Benioff (Argonne), Robert Bonneau (AFOSF), Howard Brandt (ARL), Sergey Bravyi (IBM), Bob Coecke (Oxford), Denis Ilyutko (Moscow), Louis Kauffman (Illinois), Vladimir Korepin (Stony Brook), Sam Lomonaco (Maryland), John Myers (Harvard), David Radford (Illinois) and Yong Shi Wu (Utah).

Next we would like to thank the University of Texas at Tyler for hosting the event.

Finally, the editors would like to thank the NSF for funding the conference (DMS 0901385).

Kazem Mahdavi Deborah Koslover Leonard L. Brown, III

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Yong Shi Wu University of Utah This volume contains a collection of papers, written by physicists, computer scientists, and mathematicians, from the Conference on Representation Theory, Quantum Field Theory, Category Theory, and Quantum Information Theory, which was held at the University of Texas at Tyler from October 1–4, 2009.

Quantum computing is a field at the interface of the physical sciences, computer sciences and mathematics. As such, advances in one field are often overlooked by practitioners in other fields. This volume brings together articles from each of these areas to make students, researchers and others interested in quantum computation aware of the most current advances. It is hoped that this work will stimulate future advances in the field.



