CONTEMPORARY MATHEMATICS

547

Function Spaces in Modern Analysis

Sixth Conference on Function Spaces May 18–22, 2010 Southern Illinois University, Edwardsville

> Krzysztof Jarosz Editor



American Mathematical Society

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 $10 \ 9 \ 8 \ 7 \ 6 \ 5 \ 4 \ 3 \ 2 \ 1 \\ 16 \ 15 \ 14 \ 13 \ 12 \ 11$

Contents

Preface	vii
Exponential-polynomial bases for null spaces of convolution operators in $A^{-\infty}$ A. V. Abanin, R. Ishimura, and Le Hai Khoi	1
Locally <i>m</i> -pseudoconvex algebras MATI ABEL	17
Distance Functions for Reproducing Kernel Hilbert Spaces N. Arcozzi, R. Rochberg, E. Sawyer, and B. D. Wick	25
Some properties of families of functions in $(C_b(X, \mathbb{C}), \beta)$ HUGO ARIZMENDI PEIMBERT AND ALEJANDRA GARCÍA GARCÍA	55
<i>p</i> -compact homogeneous polynomials from an ideal point of view RICHARD M. ARON AND PILAR RUEDA	61
Homomorphisms of non-commutative Banach *-algebras of Lipschitz functions FERNANDA BOTELHO AND JAMES JAMISON	73
An extension of a lemma by Phelps to Hilbert Spaces ANTONIA E. CARDWELL	79
Algebraic complements and ranges of linear operators PER H. ENFLO AND TABRINA M. SMITH	87
Wedderburn decompositions of pseudo- <i>H</i> -algebras MARINA HARALAMPIDOU	91
Spectral Preservers in Commutative Banach Algebras Osamu Hatori, Scott Lambert, Aaron Luttman, Takeshi Miura, Thomas Tonev, and Rebekah Yates	103
Spectral radii conditions for isomorphisms between unital semisimple commutative Banach algebras Go HIRASAWA, TAKESHI MIURA, AND HIROYUKI TAKAGI	125
The Peak Point Conjecture and uniform algebras invariant under group action ALEXANDER J. IZZO	s 135
Function spaces - selected open problems KRZYSZTOF JAROSZ	147

CONTENTS

Regularity, scrambling, and the steady state for stochastic matrices ROBERT KANTROWITZ, MICHAEL M. NEUMANN, AND THOMAS J.	159
KANSFORD	153
A survey of non-complex analogs of uniform algebras J. W. D. MASON	165
Properties of solution-space of the Lagrange multivariate interpolation problem using Translation-Invariant Fourier-Transformable Kernels MOHAMMED MOUATTAMID	175
On the range of composition operators on spaces of entire functions S. Mukherjee, F. Jafari, and J. E. McInroy	185
Reverse monotone approximation property TIMUR OIKHBERG	197
Biprojectivity and weak amenability of some Banach algebras HAMIDREZA RAHIMI, MAJID GHAHRAMANI, AND SAHAR MOAYERI	207
Nontrivial order preserving automorphisms of non-Archimedean fields KHODR SHAMSEDDINE	217
Composition operators between subsets of function algebras T. TONEV AND E. TONEVA	227
Function theory on certain three-manifolds JOHN WERMER	239

vi

Preface

The Sixth Conference on Function Spaces was held at Southern Illinois University at Edwardsville, from May 18 to May 22, 2010. It was attended by over one hundred participants from 25 countries. The lectures covered a broad range of topics, including spaces and algebras of analytic functions of one and of many variables (and operators on such spaces), L^p -spaces, spaces of Banach-valued functions, isometries of function spaces, geometry of Banach spaces, and other related subjects. The main purpose of the Conference was to bring together mathematicians interested in various problems within the general area of function spaces and to allow a free discussion and exchange of ideas with people working on exactly the same problems as well as with people working on related questions. Hence, most of the lectures, and therefore the papers in this volume, have been directed to non-experts. A number of articles contain an exposition of known results (known to experts) and open problems; other articles contain new discoveries that are presented in a way that should also be accessible to mathematicians working in different areas of function spaces.

The Conference was the sixth in a sequence of Conferences on Function Spaces at SIUE; the previous Conferences were held in May of 1990, 1994, 1998, 2002, and 2006. The Proceedings of the first two conferences were published with Marcel Dekker in *Lecture Notes in Pure and Applied Mathematics* series (#136 and #172), the Proceedings of the last three conference were published by the AMS in the Contemporary Mathematics series (#232, #328, and #435).

The abstracts, the schedule of the talks, and other information, as well as the pictures of the participants are available on the Conference WEB page at http://www.siue.edu/MATH/conference2010/.

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Krzysztof Jarosz

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