

Translations of
**MATHEMATICAL
MONOGRAPHS**

Volume 126

**Invariant Function Spaces
on Homogeneous Manifolds
of Lie Groups
and Applications**

M. L. Agranovskii



American Mathematical Society

Recent Titles in This Series

- 126 **M. L. Agranovskii**, Invariant function spaces on homogeneous manifolds of Lie groups and applications, 1993
- 125 **Masayoshi Nagata**, Theory of commutative fields, 1993
- 124 **Masahisa Adachi**, Embeddings and immersions, 1993
- 123 **M. A. Akivis and B. A. Rosenfeld**, Élie Cartan (1869–1951), 1993
- 122 **Zhang Guan-Hou**, Theory of entire and meromorphic functions: Deficient and asymptotic values and singular directions, 1993
- 121 **I. B. Fesenko and S. V. Vostokov**, Local fields and their extensions: A constructive approach, 1993
- 120 **Takeyuki Hida and Masuyuki Hitsuda**, Gaussian processes, 1993
- 119 **M. V. Karasev and V. P. Maslov**, Nonlinear Poisson brackets. Geometry and quantization, 1993
- 118 **Kenkichi Iwasawa**, Algebraic functions, 1993
- 117 **Boris Zilber**, Uncountably categorical theories, 1993
- 116 **G. M. Fel'dman**, Arithmetic of probability distributions, and characterization problems on abelian groups, 1993
- 115 **Nikolai V. Ivanov**, Subgroups of Teichmüller modular groups, 1992
- 114 **Seizô Itô**, Diffusion equations, 1992
- 113 **Michail Zhitomirskii**, Typical singularities of differential 1-forms and Pfaffian equations, 1992
- 112 **S. A. Lomov**, Introduction to the general theory of singular perturbations, 1992
- 111 **Simon Gindikin**, Tube domains and the Cauchy problem, 1992
- 110 **B. V. Shabat**, Introduction to complex analysis Part II. Functions of several variables, 1992
- 109 **Isao Miyadera**, Nonlinear semigroups, 1992
- 108 **Takeo Yokonuma**, Tensor spaces and exterior algebra, 1992
- 107 **B. M. Makarov, M. G. Goluzina, A. A. Lodkin, and A. N. Podkorytov**, Selected problems in real analysis, 1992
- 106 **G.-C. Wen**, Conformal mappings and boundary value problems, 1992
- 105 **D. R. Yafaev**, Mathematical scattering theory: General theory, 1992
- 104 **R. L. Dobrushin, R. Kotecký, and S. Shlosman**, Wulff construction: A global shape from local interaction, 1992
- 103 **A. K. Tsikh**, Multidimensional residues and their applications, 1992
- 102 **A. M. Il'in**, Matching of asymptotic expansions of solutions of boundary value problems, 1992
- 101 **Zhang Zhi-fen, Ding Tong-ren, Huang Wen-zao, and Dong Zhen-xi**, Qualitative theory of differential equations, 1992
- 100 **V. L. Popov**, Groups, generators, syzygies, and orbits in invariant theory, 1992
- 99 **Norio Shimakura**, Partial differential operators of elliptic type, 1992
- 98 **V. A. Vassiliev**, Complements of discriminants of smooth maps: Topology and applications, 1992
- 97 **Itiro Tamura**, Topology of foliations: An introduction, 1992
- 96 **A. I. Markushevich**, Introduction to the classical theory of Abelian functions, 1992
- 95 **Guangchang Dong**, Nonlinear partial differential equations of second order, 1991
- 94 **Yu. S. Il'yashenko**, Finiteness theorems for limit cycles, 1991
- 93 **A. T. Fomenko and A. A. Tuzhilin**, Elements of the geometry and topology of minimal surfaces in three-dimensional space, 1991
- 92 **E. M. Nikishin and V. N. Sorokin**, Rational approximations and orthogonality, 1991

(Continued in the back of this publication)

This page intentionally left blank



Invariant Function Spaces
on Homogeneous Manifolds
of Lie Groups
and Applications

This page intentionally left blank

Translations of
**MATHEMATICAL
MONOGRAPHS**

Volume 126

Invariant Function Spaces
on Homogeneous Manifolds
of Lie Groups
and Applications

M. L. Agranovskiĭ



American Mathematical Society
Providence, Rhode Island

ИНВАРИАНТНЫЕ ПРОСТРАНСТВА ФУНКЦИЙ НА ОДНОРОДНЫХ МНОГООБРАЗИЯХ ГРУПП ЛИ И ИХ ПРИЛОЖЕНИЯ

Марк Львович Аграновский

Translated by A. I. Zaslavsky from an original Russian manuscript
Translation edited by D. Louvish

The translation, editing, and keyboarding of the material for this book was done in the framework of the joint project between the AMS and Tel-Aviv University, Israel.

1991 *Mathematics Subject Classification*. Primary 43A85;
Secondary 22E46.

ABSTRACT. The monograph is devoted to the study of translation-invariant function spaces and algebras on homogeneous manifolds: semisimple and nilpotent Lie groups, Riemann symmetric spaces, bounded symmetric domains. Classification of various classes of translation-invariant spaces and algebras is obtained. Applications to characterization problems for holomorphic functions in one and several complex variables and their boundary values are given.

The monograph is directed to specialists in harmonic analysis, function theory, functional analysis, and representation theory of Lie groups.

Library of Congress Cataloging-in-Publication Data

Agranovskii, M. L. (Mark L'vovich)

[Invariantnye prostranstva funktsii na odnorodnykh mnogoobraziiakh grupp li i ikh prilozheniia. English]

Invariant function spaces on homogeneous manifolds of Lie groups and applications/
M. L. Agranovskii.

p. cm.—(Translations of mathematical monographs; v. 126)

Includes bibliographical references.

ISBN 0-8218-4604-3

1. Function spaces. 2. Harmonic analysis. 3. Semisimple Lie groups. I. Title. II. Series

QA323.A3713 1994
515'.73—dc20

93-2029
CIP

Copyright ©1993 by the American Mathematical Society. All rights reserved.

The American Mathematical Society retains all rights
except those granted to the United States Government.

The paper used in this book is acid-free and falls within the guidelines
established to ensure permanence and durability. ∞

Information on Copying and Reprinting can be found at the back of this volume.

This publication was typeset using $\mathcal{A}\mathcal{M}\mathcal{S}\text{-}\mathcal{T}\mathcal{E}\mathcal{X}$,
the American Mathematical Society's $\mathcal{T}\mathcal{E}\mathcal{X}$ macro system.

10 9 8 7 6 5 4 3 2 1 97 96 95 94 93

*To the memory
of my father*

This page intentionally left blank

Contents

Introduction	1
Chapter I. Function Spaces and Function Algebras on Differentiable Manifolds and Symmetric Spaces of Noncompact Type	5
§1. Maximal ideal spaces of antisymmetric algebras on closed differentiable manifolds	5
§2. Algebras on manifolds invariant under diffeomorphism groups	12
§3. Invariant spaces and algebras of integrable functions on symmetric spaces of noncompact type	14
§4. Invariant algebras on symmetric spaces of noncompact type	21
Chapter II. Translation Invariant Function Spaces and Function Algebras on Noncompact Lie Groups	23
§1. Invariant algebras on noncompact semisimple Lie groups	23
§2. Affine-invariant function spaces and function algebras on the Heisenberg group	31
Chapter III. Möbius Spaces and Algebras on Symmetric Domains and Their Shilov Boundaries	59
§1. Affine-invariant function algebras on Shilov boundaries of Siegel domains of the first kind	59
§2. Boundary values of holomorphic functions on the Shilov boundary of bounded symmetric domain	62
§3. Möbius spaces and algebras on Shilov boundaries of bounded symmetric domains	66
§4. Pseudounitarily invariant spaces of analytic functions on Stiefel manifolds	73
§5. Möbius subspaces of $C(\bar{D})$	89
§6. Möbius-invariant spaces in the complex ball. Separation of the \mathcal{H} -harmonic component	90
§7. Möbius $A(B^1)$ -modules in the unit disk	96

Chapter IV. Holomorphy Tests in Symmetric Domains Involving the Automorphism Group. Related Problems.	103
§1. Integral conditions for the existence of a holomorphic extension from the boundary of a symmetric domain	103
§2. Morera theorems in the unit disk for conformally invariant families of contours	106
§3. Holomorphy on invariant families of subsets of symmetric domains	113
§4. Holomorphy on a unitary-invariant family of curves in a spherical layer in \mathbb{C}^n	117
§5. The one-dimensional holomorphic extension property	121
References	127

This page intentionally left blank

References

1. M. L. Agranovskii, *Invariant algebras on the boundaries of symmetric domains*, Dokl. Akad. Nauk SSSR **197** (1971), no. 1, 9–11; English transl., Soviet Math. Doklady **12** (1971), 371–374.
2. ———, *Invariant algebras on noncompact symmetric Riemannian spaces*, Dokl. Akad. Nauk SSSR **207** (1972), no. 3, 513–516; English transl. in Soviet Math. Doklady **13** (1972).
3. ———, *On antisymmetric algebras of differentiable functions on smooth manifolds*, Sibirsk. Mat. Zh. **18** (1977), no. 2, 455–458; English transl., Siberian Math. J. **18** (1977), 327–331.
4. ———, *Fourier transform on $SL_2(\mathbb{R})$ and Morera type theorems*, Dokl. Akad. Nauk SSSR **243** (1978), no. 6, 1353–1356; English transl., Soviet Math. Doklady **19** (1978), 1522–1525.
5. ———, *Invariant function algebras on homogeneous spaces of noncompact semisimple Lie groups*, Mat. Zametki **28** (1980), no. 5, 645–652; English transl., Math. Notes **28** (1980), 779–783.
6. ———, *Tests for holomorphy in symmetric domains*, Sibirsk. Mat. Zh. **22** (1981), no. 2, 7–18; English transl., Siberian Math. J. **22** (1981), 171–179.
7. ———, *Function spaces in a disk invariant under multiplication by z and conformal translations*, Sibirsk. Mat. Zh. **22** (1981), no. 3, 3–8; English transl. in Siberian Math. J. **22** (1981).
8. ———, *Invariant spaces and traces of holomorphic functions on Shilov boundaries of the classical domains*, Sibirsk. Mat. Zh. **25** (1984), no. 2, 3–12; English transl. in Siberian Math. J. **25** (1984).
9. ———, *Invariant function algebras in symmetric spaces*, Trudy Moskov. Mat. Obshch. **47** (1984), 158–178; English transl. in Trans. Moscow Math. Soc. **47** (1985), 175–197.
10. ———, *Invariant function spaces and algebras on Lie groups and symmetric domains*, Colloquia Math. Soc. Janos Bolyai (A. Haar Memorial Conf., Budapest, 1985), vol. 49, Akademiai Kiado, Budapest, 1987, pp. 115–126.
11. ———, *Affine-invariant function algebras on the Heisenberg group*, Dokl. Akad. Nauk SSSR **289** (1986), no. 2, 265–268; English transl., Soviet Math. Doklady **34** (1987), 53–56.
12. ———, *Invariant function spaces on the Heisenberg group*, Sibirsk. Mat. Zh. **28** (1987), no. 3, 6–27; English transl., Siberian Math. J. **28** (1987), 358–375.
13. ———, *Poisson integral in Möbius-invariant spaces in the complex ball*, Siberian Math. J. **31** (1990), no. 6; English transl. in Siberian Math. J. **31** (1990).
14. M. L. Agranovskii and A. M. Semenov, *Analyticity on unitarily invariant families of curves in \mathbb{C}^n* , Sibirsk. Mat. Zh. **29** (1988), no. 1, 192–196; English transl., Siberian Math. J. **29** (1988), 149–152.
15. ———, *$SU(m, n)$ -invariant spaces of holomorphic functions*, Preprint TR90-2, University of Maryland, 1990, pp. 1–24.
16. L. A. Aizenberg and A. P. Yuzhakov, *Integral representations and residues in multidimensional complex analysis*, “Nauka”, Novosibirsk, 1988; English transl. of the 1st edition, Amer. Math. Soc., Providence, RI, 1983.

17. A. Erdélyi (ed.), *Higher transcendental functions*, McGraw-Hill, New York, 1954.
18. V. S. Vladimirov, *Methods of the theory of function of several complex variables*, "Nauka", Moscow, 1984; English transl. of the 1st edition, MIT Press, Cambridge, MA, 1966.
19. T. W. Gamelin, *Uniform algebras*, Prentice-Hall, Englewood Cliffs, NJ, 1969.
20. D. P. Zhelobenko, *Compact Lie groups and their representations*, "Nauka", Moscow, 1970; English transl., Amer. Math. Soc., Providence, RI, 1973.
21. D. P. Zhelobenko and A. I. Shtern, *Representations of Lie groups*, "Nauka", Moscow, 1983. (Russian)
22. A. A. Kirillov, *Elements of representation theory*, "Nauka", Moscow, 1972; English transl., Springer-Verlag, Berlin and New York, 1976.
23. M. M. Lavrent'ev, V. G. Romanov, and S. P. Shishatskii, *Ill posed problems of mathematical physics and analysis*, "Nauka", Moscow, 1980; English transl., Amer. Math. Soc., Providence, RI, 1986.
24. A. Barut and R. Ronczka, *Theory of group representations and applications*, vol. 2, PWN, Warszawa, 1977.
25. I. I. Pyatetskii-Shapiro, *Geometry of the classical domains and theory of automorphic functions*, "Nauka", Moscow, 1961; English transl., Gordon and Breach, New York, 1969.
26. W. Rudin, *Function theory in the unit ball of \mathbb{C}^n* , Springer-Verlag, New York, 1980.
27. G. Szegő, *Orthogonal polynomials*, 3rd edition, Amer. Math. Soc., Providence, RI, 1967.
28. S. Helgason, *Differential geometry and symmetric spaces*, Academic Press, New York, 1962.
29. E. M. Stein and G. Weiss, *Introduction to Fourier analysis on Euclidean spaces*, Princeton Univ. Press, Princeton, NJ, 1971.
30. Hua Lo-ken, *Harmonic analysis of functions of several complex variables in the classical domains*, Princeton Univ. Press, Princeton, NJ, 1963.
31. M. L. Agranovskii and R. E. Val'skii, *Maximality of invariant algebras of functions*, Sibirsk. Mat. Zh. **12** (1971), no. 1, 3–12; English transl., Siberian Math. J. **12** (1971), 1–7.
32. L. A. Aizenberg and A. Sh. Dautov, *Holomorphic functions of several complex variables with nonnegative real part. Traces of holomorphic and pluriharmonic functions on the Shilov boundary*, Mat. Sb. **99** (1976), no. 3, 342–355; English transl., Math. USSR-Sb. **28** (1976), 301–313.
33. E. B. Vinberg, S. G. Gindikin, and I. I. Pytetskii-Shapiro, *Classification and canonical realization of complex bounded homogeneous domains*, Trudy Moskov. Mat. Obshch. **12** (1963); English transl. in Trans. Moscow Math. Soc. **12** (1963) 404–437.
34. V. S. Vladimirov, *Holomorphic functions with positive imaginary part in the future tube. I*, Mat. Sb. **93** (1974), 9–17; English transl., Math. USSR-Sb. **22** (1974), 1–16.
35. V. S. Vladimirov and A. G. Sergeev, *Complex analysis in the future tube*, Sovremennye Problemy Matematiki. Fundamental'nye Napravleniya, vol. 8, VINITI, Moscow, 1985, pp. 191–266; English transl. in Encyclopaedia Math. Sci., vol. 8, Springer, Berlin and New York, 1990.
36. I. M. Gel'fand, *On subrings of the ring of continuous functions*, Uspekhi Mat. Nauk **12** (1957), no. 1, 247–251; English transl., Amer. Math. Soc. Transl. Ser. 2 **16** (1960), pp. 477–479.
37. S. G. Gindikin, *Analysis in homogeneous domains*, Uspekhi Mat. Nauk **19** (1964), no. 4, 3–92; English transl. in Russian Math. Surveys **19** (1964).
38. V. M. Gichev, *Invariant function algebras on Lie groups*, Sibirsk. Mat. Zh. **20** (1979), no. 1, 23–36; English transl., Siberian Math. J. **20** (1979), 15–25.
39. ———, *Maximal ideal spaces of invariant algebras*, Funktsional. Anal. i Prilozhen. **13** (1979), no. 3, 73–76; English transl. in Functional Anal. Appl. **13** (1979).
40. ———, *Invariant algebras of continuous functions on balls and Euclidean spaces*, Sibirsk. Mat. Zh. **25** (1984), no. 4, 32–36; English transl., Siberian Math. J. **25** (1984), 534–537.
41. E. A. Gorin, *Commutative Banach algebras generated by a group of unitary elements*, Funktsional. Anal. i Prilozhen **1** (1967), no. 3, 86–87; English transl., Functional Anal. Appl. **1** (1967), 243–244.
42. E. A. Gorin and V. M. Zolotarevskii, *Maximal subalgebras in algebras with involution*, Mat. Sb. **85** (1971), no. 3, 373–387; English transl., Math. USSR-Sb. **14** (1971), 367–382.

43. E. A. Gorin, *On the research of G. E. Shilov in the theory of commutative Banach algebras and its subsequent development*, Uspekhi Mat. Nauk **33** (1978), no. 4, 169–188; English transl., Russian Math. Surveys **33** (1978), 193–217.
44. A. M. Kytmanov, *Holomorphy criterion for integrals of Martinelli-Bochner type*, Combinatorial and Asymptotic Analysis, “Nauka”, Krasnoyarsk, 1975, pp. 169–177. (Russian)
45. N. K. Nikolskii, *Invariant subspaces in operator theory and function theory*, Itogi Nauki i Techniki, Matematicheskii Analiz, vol. 12, VINITI, Moscow, 1974, pp. 199–412; English transl. in J. Soviet Math. **5** (1976), no. 1/2.
46. P. K. Rashevskii, *Description of closed invariant subspaces of some function spaces*, Trudy Moskov. Mat. Obshch. **39** (1979), 139–185; English transl. in Proc. Moscow Math. Soc. **1981**, no. 1.
47. G. M. Henkin, *Method of integral representations in complex analysis*, Sovremennye Problemy Matematiki. Fundamental’nye Napravleniya, vol. 7, VINITI AN SSSR, Moscow, 1985, pp. 23–124; English transl., Encyclopaedia Math. Sci., vol. 7, Springer-Verlag, Berlin and New York, 1989, pp. 19–116.
48. R. O. Wells Jr., *Function theory on differentiable manifolds in \mathbb{C}^n* , Contributions to Analysis, Academic Press, New York, 1974, pp. 407–441.
49. E. M. Chirka, *Approximation by holomorphic functions on smooth manifolds in \mathbb{C}^n* , Mat. Sb. **78** (1969), no. 1, 101–123; English transl. in Math. USSR-Sb. **7** (1969).
50. G. E. Shilov, *Homogeneous rings of functions*, Uspekhi Mat. Nauk **6** (1951), no. 1, 89–135. (Russian)
51. ———, *Homogeneous rings of functions on the torus*, Dokl. Akad. Nauk SSSR **85** (1952), no. 5. (Russian)
52. J. Arazy and S. Fisher, *Some aspects of the minimal Möbius invariant space of analytic functions on the unit disk*, Interpolation spaces and related topics in analysis (Lund, 1983), Lecture Notes in Math., vol. 1070, Springer-Verlag, Berlin, 1984, pp. 24–44.
53. J. Arazy, S. Fisher, and J. Peetre, *Möbius-invariant function spaces*, J. Reine Angew. Math. **363** (1985), 110–144.
54. R. Arens, *The maximal ideals of certain function algebras*, Pacific J. Math. **8** (1958), 641–648.
55. C. A. Berenstein, *An inverse spectral theorem and its relation to the Pompeiu problem*, J. Analyse Math. **37** (1980), 128–144.
56. ———, *A test for holomorphy in the unit ball of \mathbb{C}^n* , Proc. Amer. Math. Soc. **90** (1984), no. 1, 88–90.
57. C. A. Berenstein and L. Zalcman, *Pompeiu’s problem on symmetric spaces*, Comment. Math. Helv. **55** (1980), 593–621.
58. C. A. Berenstein and M. Shahshahani, *Harmonic analysis and the Pompeiu problem*, Amer. J. Math. **105** (1983), no. 5, 1217–1229.
59. A. G. Brandstein, *Compact 2-manifolds as maximal ideal spaces*, Proc. Amer. Math. Soc. **41** (1973), no. 2, 438–450.
60. J.-E. Björk, *Compact groups operating on Banach algebra*, Math. Ann. **205** (1973), no. 4, 281–297.
61. J. Delsart, *Note sur une propriété nouvelle des fonctions harmoniques*, C. R. Acad. Sci. Paris Ser. I Math. **246** (1958), 1358–1360.
62. J. Delsart and J. L. Lions, *Moyennes généralisées*, Comment. Math. Helv. **33** (1959), 59–69.
63. L. M. Druzkowski, *Continuous holomorphic extension from the boundary in Banach space*, Proc. Intern. Conf. on Complex Anal. and Appl., Varna, 1981, pp. 157–160.
64. M. Educhi, M. Hashirime, and K. Okamoto, *The Paley-Wiener theorem for distributions on symmetric space*, Hiroshima Math. J. **3** (1973), no. 1, 109–120.
65. M. Freeman, *Uniform approximation on a real analytic manifold*, Trans. Amer. Math. Soc. **143** (1969), 545–553.
66. G. B. Folland and E. M. Stein, *Hardy spaces on homogeneous groups M* , Math. Notes **28**, Princeton Univ. Press, Princeton, NJ, 1982.
67. R. Gangolli, *Invariant function algebras on compact semisimple Lie groups*, Bull. Amer. Math. Soc. **71** (1965), no. 3, 634–637.

68. J. Globevnik, *On boundary values of holomorphic functions on balls*, Proc. Amer. Math. Soc. **85** (1982), 61–64.
69. ———, *On holomorphic extensions from spheres in \mathbb{C}^2* , Proc. Roy. Soc. Edinburg **94A** (1983), 113–120.
70. ———, *A family of lines for testing holomorphy in the ball of \mathbb{C}^2* , preprint, vol. 24, Ljubljana Univ., Ljubljana, 1986.
71. ———, *Analyticity on rotation invariant families of curves*, Trans. Amer. Math. Soc. **280** (1983), 247–254.
72. D. Geller, *Fourier analysis on the Heisenberg group*, Proc. Nat. Acad. Sci. U.S.A. **74** (1977), 1328–1331.
73. E. Grinberg, *Boundary values of holomorphic functions, Radon transform and the one dimensional extension property*, preprint, Temple University, 1985.
74. ———, *A boundary analogue of Morera's theorem in the unit ball of \mathbb{C}^n* , Proc. Amer. Math. Soc. **102** (1988), no. 1, 114–116.
75. L. R. Hunt and R. O. Wells, Jr., *Extension of CR-functions*, Amer. J. Math. **98** (1976), 805–820.
76. L. Hörmander and J. Wermer, *Uniform approximation on compact sets in \mathbb{C}^n* , Math. Scand. **23** (1968), no. 1, 5–21.
77. K. D. Johnson, *On a ring of invariant polynomials on a Hermitian symmetric space*, J. Algebra **67** (1980), 72–81.
78. S. Kobayashi, *Fixed points of isometries*, Nagoya Math. J. **13** (1958), 63–68.
79. A. Koranyi, *Poisson integral and boundary components of symmetric spaces*, Invent. Math. **34** (1976), 19–34.
80. K. de Leeuw and H. Mirkil, *Intrinsic algebras on the torus*, Trans. Amer. Math. Soc. **81** (1956), 320–330.
81. ———, *Translation-invariant function algebras on abelian groups*, Bull. Soc. Math. France **88** (1960), 345–370.
82. ———, *Rotation-invariant algebras on the n -sphere*, Duke Math. J. **30** (1961), no. 4, 667–672.
83. ———, *Algebras of differentiable functions in the plane*, Ann. Inst. Fourier (Grenoble) **13** (1963), no. 2, 75–90.
84. A. Nagel and W. Rudin, *Möbius-invariant function spaces on balls and spheres*, Duke Math. J. **43** (1976), 841–865.
85. R. D. Ogden and S. Vagi, *Harmonic analysis on a nilpotent group and function theory of Siegel domains of type II*, Adv. in Math. **33** (1979), no. 1, 31–92.
86. J. Peetre, *Invariant function spaces—a rapid survey*, technical report (1985), Lund.
87. ———, *Paracommutators and minimal spaces*, Operators and function theory, Reidel, Dordrecht, 1985, pp. 163–224.
88. D. Rider, *Translation-invariant Dirichlet algebras on compact groups*, Proc. Amer. Math. Soc. **17** (1966), no. 5, 977–985.
89. W. Rudin, *Unitarily invariant algebras of continuous functions on spheres*, Houston J. Math. **5** (1979), 253–265.
90. ———, *Möbius-invariant algebras in balls*, Ann. Inst. Fourier (Grenoble) **33** (1983), no. 2, 19–41.
91. ———, *Eigenspaces of invariant Laplacian in B^n* , J. Analyse Math. **43** (1983/1984), 136–148.
92. L. A. Rubel, *Möbius-invariant spaces of continuous functions*, Bull. Greek Math. Soc. **20** (1979), 94–97.
93. ———, *Harmonic analysis of harmonic functions in the plane*, Proc. Amer. Math. Soc. **54** (1976), no. 1, 146–148.
94. L. A. Rubel and A. L. Shields, *Invariant subspaces of L^∞ and H^∞* , J. Reine Angew. Math. **272** (1975), 32–44.
95. L. A. Rubel and R. M. Timoney, *An extremal property of the Bloch space*, Proc. Amer. Math. Soc. **75** (1979), 45–49.
96. E. L. Stout, *The boundary values of holomorphic functions of several complex variables*, Duke Math. J. **44** (1977), 105–108.

97. W. Schmid, *Die Randwerte holomorpher Funktionen und hermitesche symmetrischen Räumen*, *Invent. Math.* **9** (1969/70), 61–80.
98. L. Schwartz, *Théorie générale des fonctions moyenne-périodiques*, *Ann. of Math.* **42** (1947), 857–929.
99. M. Takeuchi, *Polynomial representations associated with bounded symmetric domains*, *Osaka J. Math.* **10** (1973), 441–445.
100. R. M. Timoney, *Maximal invariant spaces of analytic functions*, *Indiana Univ. J. Math.* **31** (1982), 651–664.
101. J. A. Tirao, *Self-adjoint function spaces on Riemannian symmetric spaces*, *Proc. Amer. Math. Soc.* **24** (1970), 223–228.
102. J. Wermer, *Approximation on a disk*, *Math. Ann.* **155** (1964), 331–333.
103. ———, *Polynomially convex disks*, *Math. Ann.* **158** (1965), 6–10.
104. J. A. Wolf, *Selfadjoint function spaces on Riemann symmetric spaces*, *Proc. Amer. Math. Soc.* **113** (1964), 299–315.
105. ———, *Translation-invariant function algebras on compact groups*, *Pacific J. Math.* **15** (1965), no. 3, pp. 1093–1099.
106. L. Zalcman, *Analyticity and the Pompeiu problem*, *Arch. Rational Mech. Anal.* **47** (1972), 237–254.
107. ———, *Offbeat integral geometry*, *Amer. Math. Monthly* **87** (1980), no. 3, 161–175.

References added for the English edition

108. Y. Beniamini and Y. Weit, *Harmonic analysis of spherical functions on $SU(1, 1)$* , *Ann. Inst. Fourier (Grenoble)* **42** (1992), no. 3, 671–694.
109. Y. Globevnik and E. L. Stout, *Boundary Morera theorems for holomorphic functions of several complex variables*, *Duke Math. J.* **64** (1991), 571–615.
110. M. L. Agranovskii and A. M. Semenov, *Boundary analogues of Hartogs' theorem*, *Siberian Math. J.* **32** (1991), no. 1.
111. C. Berenstein, D. C. Chang, D. Pascus, and L. Zalcman, *Variation on the theorem of Morera*, *Contemporary Math.* (1992, to appear).
112. M. L. Agranovskii, C. Berenstein, D. C. Chang, and D. Pascus, *A Morera type theorem for L^2 -functions in the Heisenberg group*, *J. Analyse Math.* **57** (1991).
113. ———, *Théorèmes de Morera et Pompeiu pour le groupe de Heisenberg*, *C. R. Acad. Sci. Paris Sér. I Math.* (1992, to appear).
114. M. L. Agranovskii, C. Berenstein, and D. C. Chang, *Morera theorem for holomorphic H^p -spaces in the Heisenberg group*, *J. Reine Angew. Math.* (to appear).
115. S. Thangavelu, *Spherical means and CR functions on the Heisenberg group*, *J. Analyse Math.* (to appear).
116. J. Faraut and A. Koranyi, *Function spaces and reproducing kernels on bounded symmetric domain*, *J. Funct. Anal.* **88** (1990), no. 1, 64–89.
117. J. Arazy, *Realization of the invariant inner product on the highest quotients of the composition series*, *Ark. Mat.* **30** (1992), no. 1, 1–24.

This page intentionally left blank

Recent Titles in This Series

(Continued from the front of this publication)

- 91 **Mamoru Mimura and Hiroshi Toda**, Topology of Lie groups, I and II, 1991
- 90 **S. L. Sobolev**, Some applications of functional analysis in mathematical physics, third edition, 1991
- 89 **Valerii V. Kozlov and Dmitrii V. Treshchëv**, Billiards: A genetic introduction to the dynamics of systems with impacts, 1991
- 88 **A. G. Khovanskii**, Fewnomials, 1991
- 87 **Aleksandr Robertovich Kemer**, Ideals of identities of associative algebras, 1991
- 86 **V. M. Kadets and M. I. Kadets**, Rearrangements of series in Banach spaces, 1991
- 85 **Mikio Ise and Masaru Takeuchi**, Lie groups I, II, 1991
- 84 **Đáo Trọng Thi and A. T. Fomenko**, Minimal surfaces, stratified multivarifolds, and the Plateau problem, 1991
- 83 **N. I. Portenko**, Generalized diffusion processes, 1990
- 82 **Yasutaka Sibuya**, Linear differential equations in the complex domain: Problems of analytic continuation, 1990
- 81 **I. M. Gelfand and S. G. Gindikin, Editors**, Mathematical problems of tomography, 1990
- 80 **Junjiro Noguchi and Takushiro Ochiai**, Geometric function theory in several complex variables, 1990
- 79 **N. I. Akhiezer**, Elements of the theory of elliptic functions, 1990
- 78 **A. V. Skorokhod**, Asymptotic methods of the theory of stochastic differential equations, 1989
- 77 **V. M. Filippov**, Variational principles for nonpotential operators, 1989
- 76 **Phillip A. Griffiths**, Introduction to algebraic curves, 1989
- 75 **B. S. Kashin and A. A. Saakyan**, Orthogonal series, 1989
- 74 **V. I. Yudovich**, The linearization method in hydrodynamical stability theory, 1989
- 73 **Yu. G. Reshetnyak**, Space mappings with bounded distortion, 1989
- 72 **A. V. Pogorelev**, Bendings of surfaces and stability of shells, 1988
- 71 **A. S. Markus**, Introduction to the spectral theory of polynomial operator pencils, 1988
- 70 **N. I. Akhiezer**, Lectures on integral transforms, 1988
- 69 **V. N. Salii**, Lattices with unique complements, 1988
- 68 **A. G. Postnikov**, Introduction to analytic number theory, 1988
- 67 **A. G. Dragalin**, Mathematical intuitionism: Introduction to proof theory, 1988
- 66 **Ye Yan-Qian**, Theory of limit cycles, 1986
- 65 **V. M. Zolotarev**, One-dimensional stable distributions, 1986
- 64 **M. M. Lavrent'ev, V. G. Romanov, and S. P. Shishat'skii**, Ill-posed problems of mathematical physics and analysis, 1986
- 63 **Yu. M. Berezanskii**, Selfadjoint operators in spaces of functions of infinitely many variables, 1986
- 62 **S. L. Krushkal', B. N. Apanasov, and N. A. Gusevskii**, Kleinian groups and uniformization in examples and problems, 1986
- 61 **B. V. Shabat**, Distribution of values of holomorphic mappings, 1985
- 60 **B. A. Kushner**, Lectures on constructive mathematical analysis, 1984
- 59 **G. P. Egorychev**, Integral representation and the computation of combinatorial sums, 1984
- 58 **L. A. Aizenberg and A. P. Yuzhakov**, Integral representations and residues in multidimensional complex analysis, 1983

(See the AMS catalog for earlier titles)

COPYING AND REPRINTING. Individual readers of this publication, and non-profit libraries acting for them, are permitted to make fair use of the material, such as to copy a chapter for use in teaching or research. Permission is granted to quote brief passages from this publication in reviews, provided the customary acknowledgment of the source is given.

Republication, systematic copying, or multiple reproduction of any material in this publication (including abstracts) is permitted only under license from the American Mathematical Society. Requests for such permission should be addressed to the Manager of Editorial Services, American Mathematical Society, P.O. Box 6248, Providence, Rhode Island 02940-6248.

The owner consents to copying beyond that permitted by Sections 107 or 108 of the U.S. Copyright Law, provided that a fee of \$1.00 plus \$.25 per page for each copy be paid directly to the Copyright Clearance Center, Inc., 27 Congress Street, Salem, Massachusetts 01970. When paying this fee please use the code 0065-9282/93 to refer to this publication. This consent does not extend to other kinds of copying, such as copying for general distribution, for advertising or promotional purposes, for creating new collective works, or for resale.

ISBN 0-8218-4604-3



9 780821 846049