

Nonlinear Functional Analysis and Its Applications

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SYMPOSIA IN
PURE MATHEMATICS**

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NONLINEAR FUNCTIONAL ANALYSIS
AND ITS APPLICATIONS

PROCEEDINGS OF SYMPOSIA
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Nonlinear Functional Analysis and Its Applications

Felix E. Browder, Editor

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Contents

PART 1

Foreword	xi
A note on the regularity of solutions obtained by global topological methods J. C. ALEXANDER	1
Asymmetric rotating wave solutions of reaction-diffusion equations J. C. ALEXANDER	7
Parabolic evolution equations with nonlinear boundary conditions HERBERT AMANN	17
Nonlinear oscillations with minimal period ANTONIO AMBROSETTI	29
On steady Navier–Stokes flow past a body in the plane CHARLES J. AMICK	37
On a contraction theorem and applications IOANNIS K. ARGYROS	51
Dual variational principles for eigenvalue problems GILES AUCHMUTY	55
Generalized elliptic solutions of the Dirichlet problem for n -dimensional Monge–Ampère equations ILYA J. BAKELMAN	73
Existence and containment of solutions to parabolic systems PETER W. BATES	103
Periodic Hamiltonian trajectories on starshaped manifolds HENRI BERESTYCKI, JEAN-MICHEL LASRY, GIANNI MANCINI and BERNHARD RUF	109
Integrability of nonlinear differential equations via functional analysis M. S. BERGER, P. T. CHURCH and J. G. TIMOURIAN	117
Extinction of the solutions of some quasilinear elliptic problems of arbitrary order F. BERNIS	125
On a system of degenerate diffusion equations M. BERTSCH, M. E. GURTIN, D. HILHORST and L. A. PELETIER	133
Pointwise continuity for a weak solution of a parabolic obstacle problem MARCO BIROLI	141
A note on iteration for pseudoparabolic equations of fissured media type MICHAEL BÖHM	147

Homogenization of two-phase flow equations ALAIN BOURGEAT	157
Some variational problems with lack of compactness HAIM BREZIS	165
Degree theory for nonlinear mappings FELIX E. BROWDER	203
Construction of periodic solutions of periodic contractive evolution systems from bounded solutions RONALD E. BRUCK	227
An abstract critical point theorem for strongly indefinite functionals A. CAPOZZI and D. FORTUNATO	237
Uniqueness of positive solutions for a sublinear Dirichlet problem ALFONSO CASTRO	243
Applications of homology theory to some problems in differential equations KUNG-CHING CHANG	253
On the continuation method and the method of monotone iterations PHILIPPE CLÉMENT	263
Existence theorems for superlinear elliptic Dirichlet problems in exterior domains CHARLES V. COFFMAN and MOSHE M. MARCUS	271
A global fixed point theorem for symplectic maps and subharmonic solu- tions of Hamiltonian equations on tori C. CONLEY and E. ZEHNDER	283
Harmonic maps from the disk into the Euclidean N -sphere JEAN-MICHEL CORON	301
Nonlinear semigroups and evolution governed by accretive operators MICHAEL G. CRANDALL	305
A theorem of Mather and the local structure of nonlinear Fredholm maps JAMES DAMON	339
Remarks on S^1 symmetries and a special degree for S^1 -invariant gradient mappings E. N. DANCER	353
Abstract differential equations, maximal regularity, and linearization G. DA PRATO	359
Positive solutions for some classes of semilinear elliptic problems DJAIRÓ G. DE FIGUEIREDO	371
Elliptic and parabolic quasilinear equations giving rise to a free boundary: the boundary of the support of the solutions JESUS ILDEFONSO DIAZ	381
An index theory for periodic solutions of convex Hamiltonian systems I. EKELAND	395

An extension of the Leray–Schauder degree for fully nonlinear elliptic problems	
P. M. FITZPATRICK and JACOBO PEJSACHOWICZ	425
Nonlinear special manifolds for the Navier–Stokes equations	
C. FOIAS and J. C. SAUT	439
Regularity criteria for weak solutions of the Navier–Stokes system	
YOSHIKAZU GIGA	449
A strongly nonlinear elliptic problem in Orlicz–Sobolev spaces	
JEAN-PIERRE GOSSEZ	455
Nontrivial solutions of semilinear elliptic equations of fourth order	
YONG-GENG GU	463
Approximation in Sobolev spaces and nonlinear potential theory	
LARS INGE HEDBERG	473
Some free boundary problems for predator-prey systems with nonlinear diffusion	
JESÚS HERNÁNDEZ	481
On positive solutions of semilinear periodic-parabolic problems	
PETER HESS	489
The topological degree at a critical point of mountain-pass type	
HELMUT HOFER	501
On a conjecture of Lohwater about asymptotic values of meromorphic functions	
J. S. HWANG	511
Parametrix of \square_b	
CHISATO IWASAKI	521
Applications of Nash–Moser theory to nonlinear Cauchy problems	
NOBUHISA IWASAKI	525
Nonlinear multiparametric equations: structure and topological dimension of global branches of solutions	
J. IZE, I. MASSABÓ, J. PEJSACHOWICZ and A. VIGNOLI	529

PART 2

Remarks on the Euler and Navier–Stokes equations in \mathbf{R}^2	
TOSIO KATO	1
Nonlinear equations of evolution in Banach spaces	
TOSIO KATO	9
Geometrical properties of level sets of solutions to elliptic problems	
BERNHARD KAWOHL	25
Remarks about St. Venant solutions in finite elasticity	
DAVID KINDERLEHRER	37

Nonexpansive mappings in product spaces, set-valued mappings and k -uniform rotundity W. A. KIRK	51
A new operator theoretic algorithm for solving first order scalar quasilinear equations YOSHIKAZU KOBAYASHI	65
A general interpolation theorem of Marcinkiewicz type HIKOSABURO KOMATSU	77
An easy proof of the interior gradient bound for solutions to the prescribed mean curvature equation N. KOREVAAR	81
On application of the monotone iteration scheme to wave and biharmonic equations PHILIP KORMAN	91
Unilateral obstacle problem for strongly nonlinear second order elliptic operators RÜDIGER LANDES and VESA MUSTONEN	95
Product formula, imaginary resolvents and modified Feynman integral MICHEL L. LAPIDUS	109
Quasilinear elliptic equations with nonlinear boundary conditions GARY M. LIEBERMAN	113
Some L^p inequalities and their applications to fixed point theorems of uniformly Lipschitzian mappings TECK-CHEONG LIM	119
Some remarks on the optimal control of singular distributed systems J. L. LIONS	127
Global continuation and complicated trajectories for periodic solutions of a differential-delay equation JOHN MALLET-PARET and ROGER D. NUSSBAUM	155
On quasiconvexity in the calculus of variations PAOLO MARCELLINI	169
Asymptotic growth for evolutionary surfaces of prescribed mean curvature PAOLO MARCELLINI and KEITH MILLER	175
L^2 -decay of solutions of the Navier–Stokes equations in the exterior domain KYÛYA MASUDA	179
On the index and the covering dimension of the solution set of semilinear equations P. S. MILOJEVIĆ	183
Pointwise potential estimates for elliptic obstacle problems UMBERTO MOSCO	207
On singularities of solutions to nonlinear elliptic systems of partial differential equations JINDŘICH NEČAS	219

Uniqueness, nonuniqueness and related questions of nonlinear elliptic and parabolic equations WEI-MING NI	229
Global solutions of the hyperbolic Yang–Mills equations and their sharp asymptotics STEPHEN M. PANEITZ	243
Surjectivity of generalized ϕ -accretive operators SEHIE PARK and JONG AN PARK	255
Approximation-solvability of periodic boundary value problems via the A -proper mapping theory W. V. PETRYSHYN	261
On a generalization of the Fuller index A. J. B. POTTER	283
Minimax methods for indefinite functionals PAUL H. RABINOWITZ	287
Nonlinear semigroups, holomorphic mappings and integral equations SIMEON REICH	307
Rearrangement of functions and reverse Jensen inequalities CARLO SBORDONE	325
Bifurcation and even-like vector fields STEVE J. SCHIFFMAN and JAY H. WOLKOWISKY	331
Classical and quantized invariant wave equations—progress and problems IRVING SEGAL	341
Resonance and the stationary Navier–Stokes equations VICTOR L. SHAPIRO	359
On removable point singularities of coupled Yang–Mills fields L. M. SIBNER	371
Two-function minimax theorems and variational inequalities for functions on compact and noncompact sets, with some comments on fixed-point theorems S. SIMONS	377
On approximating fixed points S. P. SINGH and B. WATSON	393
Symmetry breaking and nondegenerate solutions of semilinear elliptic equations JOEL A. SMOLLER and ARTHUR G. WASSERMAN	397
A generalized Palais-Smale condition and applications MICHAEL STRUWE	401
Existence and nonuniqueness of solutions of a noncoercive elliptic variational inequality ANDRZEJ SZULKIN	413

Fixed point, minimax, and Hahn-Banach theorems WATARU TAKAHASHI	419
Remarks on the Euler equations R. TEMAM	429
Infinite-dimensional dynamical systems in fluid mechanics R. TEMAM	431
Existence of symmetric homoclinic orbits for systems of Euler-Lagrange equations J. F. TOLAND	447
Graphs with prescribed curvature NEIL S. TRUDINGER	461
Navier-Stokes equations for compressible fluids: global estimates and periodic solutions ALBERTO VALLI	467
Weak and strong singularities of nonlinear elliptic equations LAURENT VÉRON	477
Regularity of weak solutions of the Navier-Stokes equations WOLF VON WAHL	497
A monotone convergence theorem in abstract Banach spaces IOAN I. VRABIE	505
On a class of strongly nonlinear Dirichlet boundary-value problems: beyond Pohožaev's results PIERRE A. VUILLERMOT	521
Topological degree and global bifurcation JEFFREY R. L. WEBB and STEWART C. WELSH	527
Generalized idea of Synge and its applications to topology and calculus of variations in positively curved manifolds S. WALTER WEI	533
On extending the Conley-Zehnder fixed point theorem to other manifolds ALAN WEINSTEIN	541
L^p -energy and blow-up for a semilinear heat equation FRED B. WESSLER	545
A geometric theory of bifurcation JAY H. WOLKOWISKY	553
Some problems on degenerate quasilinear parabolic equations ZHUOQUN WU	565
Quasi-homogeneous microlocal analysis for nonlinear partial differential equations MASAO YAMAZAKI	573

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