

The Arcata Conference on Representations of Finite Groups

Volume 47 - Part 2

**PROCEEDINGS OF
SYMPOSIA IN
PURE MATHEMATICS**

AMERICAN MATHEMATICAL SOCIETY

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IN PURE MATHEMATICS
Volume 47, Part 2

The Arcata Conference
on Representations
of Finite Groups

Paul Fong, Editor

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