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Applied Problems of Radon Transform

Simon Gindikin
Editor



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Applied Problems of Radon Transform

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Editor



American Mathematical Society
Providence, Rhode Island

С. Г. Гиндикин (редактор)
Приложения преобразования Радона

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ABSTRACT. The aim of this collection is to acquaint the reader with recent work in this area that was done in what was formerly the Soviet Union. The papers in this collection are devoted to mathematical problems that are related to applications. In some cases these problems are problems of practical tomography; in other cases they are theoretical problems that originated in tomography. However, in all these papers the main emphasis is on the mathematical aspects of the problem.

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