American Mathematical Society

## TRANSLATIONS

Series 2 • Volume 201

Advances in the Mathematical Sciences

# L. D. Faddeev's Seminar on Mathematical Physics

Michael Semenov-Tian-Shansky Editor



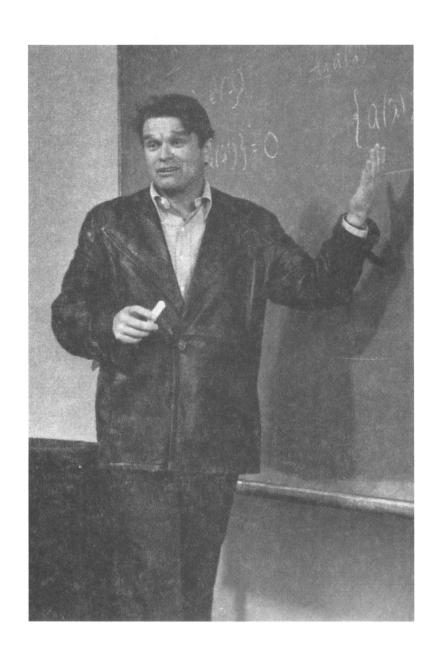
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(Continued in the back of this publication)



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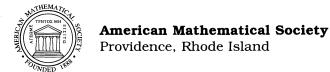
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Advances in the Mathematical Sciences—49

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## L. D. Faddeev's Seminar on Mathematical Physics

Michael Semenov-Tian-Shansky Editor



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10 9 8 7 6 5 4 3 2 1 05 04 03 02 01 00

### Contents

Some personal historic notes on our seminar	
Michael Semenov-Tian-Shansky	1
An elementary derivation of certain classical dynamical $r$ -matrices A. Alekseev and E. Meinrenken	9
Incidence matrix description of intersecting $p$ -brane solutions I. Ya. Aref'eva and O. A. Rytchkov	19
A discrete time Lagrange top and discrete elastic curves A. I. Bobenko and Yu. B. Suris	39
The Gelfand-Levitan-Marchenko equation and the long-time asymptotics of the solutions of the nonlinear Schrödinger equation A. M. Budylin and V. S. Buslaev	63
From the tetrahedron equation to universal R-matrices R. M. KASHAEV AND A. YU. VOLKOV	79
On some quadratic algebras A. N. Kirillov	91
Quantum inverse scattering method and correlation functions V. Korepin and N. Slavnov	115
Testing Seiberg-Witten solution A. Losev, N. Nekrasov, and S. Shatashvili	123
Drinfeld twists and algebraic Bethe Ansatz J. M. MAILLET AND SANCHEZ DE SANTOS	137
Darboux transformations, covariance theorems and integrable systems V. B. Matveev	179
Generalized q-deformed Gelfand-Dickey structures on the group of q-pseudodifference operators A. L. Pirozerski and M. A. Semenov-Tian-Shansky	211
11. 2. 1 HOSSIGH HID III. 11. DEMENOV I'M DIMIGHT	

viii CONTENTS

On time evolutions associated with the nonstationary Schrödinger equation A. K. Pogrebkov	239
Deformation quantization of Kähler manifolds N. RESHETIKHIN AND L. A. TAKHTAJAN	257
Canonicity of Bäcklund transformation: $r$ -matrix approach. I E. K. Sklyanin	277
Quasi-classical study of form factors in finite volume F. A. SMIRNOV	283
Completeness of the hypergeometric solutions of the $qKZ$ equation at level zero V. Tarasov	309



### Selected Titles in This Subseries

(Continued from the front of this publication)

- 23 Yu. Ilyashenko and S. Yakovenko, Editors, Concerning the Hilbert 16th Problem (TRANS2/165)
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