NOTE ON THE DEFINING RELATIONS FOR THE SIMPLE GROUP OF ORDER 660

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Dickson* has given the following set of defining relations for the simple group of order 660:

- (1) $S^{11} = I, \quad T^2 = I, \quad (ST)^3 = I,$
- (2) $(S^3TS^8T)^2 = I,$
- (3) $(S^4TS^6T)^2 = I.$

It follows from (3) that

$$TS^4T = S^5TS^7TS^5,$$

so that

$$TS^{8}T = S^{5}TS^{7}TS^{10}TS^{7}TS^{5}$$

= $S^{5}TS^{8} \cdot S^{-1}TS^{-1}TS^{-1} \cdot S^{8}TS^{5}$
= $S^{5}TS^{8}TS^{8}TS^{5}$.

From this last relation

$$S^{3}TS^{5}TS^{5} \cdot S^{3}TS^{8}T \cdot S^{5}T = I,$$

$$S^{3}TS^{8}T = S^{6}TS^{6}TS^{8}TS^{6},$$

$$(S^{3}TS^{8}T)^{2} = S^{6}TS^{6}TS^{8}TST^{6}TS^{8}TS^{6}$$

$$= S^{6}TS^{6}TS^{7} \cdot STSTS \cdot S^{5}TS^{8}TS^{6}$$

$$= S^{6}TS^{6} \cdot TS^{7}TS^{5}T \cdot S^{8}TS^{6}$$

$$= S^{6}TS^{6} \cdot S^{6}TS^{4} \cdot S^{8}TS^{6}$$

$$= S^{6}TSTSTS^{6}$$

$$= I.$$

Since (2) has been derived from (1) and (3), it follows that (1) and (3) are sufficient to define the simple group of order 660.

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